

Rotor Airload and Acoustics Prediction Based on CFD/CSD Coupling Method

Wang Liangquan, Xu Guohua*, Shi Yongjie

National Key Laboratory of Science and Technology on Rotorcraft Aeromechanics, Nanjing University of Aeronautics and Astronautics, Nanjing 210016, P. R. China

(Received 22 February 2017; revised 27 April 2017; accepted 19 July 2017)

Abstract: An advanced airload and noise prediction method based on computational fluid dynamics/computational structural dynamics (CFD/CSD) coupling for helicopter rotor has been developed in this paper. In the present method, Navier-Stokes equation is applied as the governing equation, and a moving overset grid system is generated in order to account for the blade motions in rotation, flapping and pitching. The blade structural analysis is based on 14-DOF Euler beam model, and the finite element discretization is conducted on Hamilton's variational principle and moderate deflection theory. Aerodynamic noise is calculated by Farassat 1A formula derived from FW-H equation. Using the developed method, numerical example of UH-60A is performed for aeroelastic loads calculation in a low-speed forward flight, and the calculated results are compared with both those from isolated CFD method and available experimental data. Then, rotor noise is emphatically calculated by CFD/CSD coupling method and compared with the isolated CFD method. The results show that the aerodynamic loads calculated from CFD/CSD method are more satisfactory than those from isolated CFD method, and the exclusion of blade structural deformation in rotor noise calculation may cause inaccurate results in low-speed forward flight state.

Key words: helicopter; rotor; airload; aerodynamic noise; computational fluid dynamics (CFD); computational structural dynamics (CSD)

CLC number: V211.52 **Document code:** A **Article ID:** 1005-1120(2018)02-0343-10

0 Introduction

Helicopters present the unique capability to hover and fly at very low speeds to perform complex tasks. Rotor is the most important aerodynamic component of a helicopter, providing lift, propulsion and control^[1]. The capability of the rotor comes at the expense of significant noise. When a rotor operates in a low-speed forward or descent flight, tip vortices shed from the preceding blades move close to the following blades, which may lead to strong blade-vortex interaction (BVI) noise. BVI noise is the major source of annoyance^[2]. It is of great significance to study the unsteady aerodynamic loads and noise when the rotor is at a BVI condition.

Prescribed wake and free wake methods were

used to calculate the induced velocities of rotor in previous studies, and the results were not satisfactory. With the rapid development of computer capability, rotor computational fluid dynamics (CFD) method with rigid blade assumption has gradually played an important role. The governing equations for solving flowfield evolve from transonic small disturbance (TSD) to Navier-Stokes (N-S) equations^[3]. Due to the complexity of CFD solution, blade structural deformation was not taken into account before mid-1980's. Actually, when a helicopter rotor operates in forward flight, the aerodynamic loads on blade will be affected by its elastic deformation. In 1986, Tung et al.^[4] first carried out CFD and CSD coupling research, and a TSD code was coupled with

* Corresponding author, E-mail address: ghxu@nuaa.edu.cn.

How to cite this article: Wang Liangquan, Xu Guohua, Shi Yongjie. Rotor airload and acoustics prediction based on CFD/CSD coupling method[J]. Trans. Nanjing Univ. Aero. Astro., 2018, 35(2): 343-352.

<http://dx.doi.org/10.16356/j.1005-1120.2018.02.343>

comprehensive analytical model of rotorcraft aerodynamics and dynamics (CAMRAD) by them. Pomin and Wagner calculated the airloads of the hovering Helishape 7A model rotor and a forward flight Caradonna-Tung (CTung) rotor^[5]. In their research, Timoshenko beam theory was adopted in the CSD module, and the results showed better correlation with measured data than rigid blade computations about rotor thrust and torque coefficients. In 2008, Sitaraman et al.^[6] predicted the rotor maneuver loads using CFD/CSD analysis. CFD and CSD solvers in their study were transonic unsteady rotor Navier-Stokes (TURNS) and DYMORE, respectively. Ref. [7] assessed the state-of-art of CFD/CSD codes using the HART II data. CFD/CSD method was also used for rotor aerodynamic noise prediction in recent years^[8-9].

In the research of rotor aerodynamic noise, Williams and Hawkins derived the FW-H equation which governs the noise radiated from a solid body in arbitrary motion in Ref. [10]. When the blade tip speed is subsonic, the contribution of quadrupole term to rotor noise is negligible, and the quadrupole term could be omitted in the right-hand side of the FW-H equation. Thus monopole term and dipole term remain, which can be interpreted as thickness noise and loading noise source term. In the present investigation, the widely used F1A formula derived from FW-H equation by Farassat^[11] is adopted for noise analysis.

Domestic studies on this field are lag comparatively. Wang et al.^[12-13] established CFD/CSD coupling method to calculate rotor airloads without involving rotor noise. Shi et al.^[14] investigated the noise abatement level of advanced blade tip without considering blade elasticity. In order to understand the influence of blade deformation on rotor noise, this paper develops a new rotor aerodynamic noise prediction method by combining CFD/CSD coupling model with the F1A formula. The UH-60A helicopter is taken as a numerical example, and the computations of flow-field and noise are performed in a low-speed for-

ward flight. A structured moving overset grid system is generated and the CFD solution is based on Reynolds-Averaged Navier-Stokes (RANS) equations. The CSD solution is based on Euler-Bernoulli beam model and Hamilton's variational principle. The elastic deformation of the blade grid is achieved by an algebraic method. Besides, the airloads and structural deformations between CFD and CSD module are transferred via interpolation. The results indicate that the normal force coefficients calculated by CFD/CSD are more accurate than that by isolated CFD method, and their difference of noise level can be up to 5 dB at some observer positions.

1 Numerical Methods

1.1 Rotor CFD model

N-S equations for three-dimensional unsteady compressible flows in conservative form are given by^[15]

$$\frac{\partial}{\partial t} \int_{\Omega} \mathbf{W} d\Omega + \oint_{\partial\Omega} (\mathbf{F}_c - \mathbf{F}_v) dS = 0 \quad (1)$$

where Ω is the control volume, \mathbf{W} the conservative variables, \mathbf{F}_c and \mathbf{F}_v the convective and the viscous fluxes, respectively. Their expressions are as follows

$$\mathbf{W} = [\rho \quad \rho u \quad \rho v \quad \rho w \quad \rho E]^T \quad (2)$$

$$\mathbf{F}_c = \begin{bmatrix} \rho V \\ \rho u V + n_x p \\ \rho v V + n_y p \\ \rho w V + n_z p \\ \rho H V \end{bmatrix} \quad (3)$$

$$\mathbf{F}_v = \begin{bmatrix} 0 \\ n_x \tau_{xx} + n_y \tau_{xy} + n_z \tau_{xz} \\ n_x \tau_{yx} + n_y \tau_{yy} + n_z \tau_{yz} \\ n_x \tau_{zx} + n_y \tau_{zy} + n_z \tau_{zz} \\ n_x \Theta_x + n_y \Theta_y + n_z \Theta_z \end{bmatrix} \quad (4)$$

The spatial discretization of the governing equations is achieved by Jameson central scheme. The dual time-stepping approach is implemented, and explicit Runge-Kutta method is employed at each pseudo time step. The turbulence model adopted in the present analysis is Baldwin-Lomax

model. In order to improve the calculation efficiency, the background Cartesian grid is divided into several blocks and the MPI parallel strategy is used.

1.2 Rotor CSD model

Blade structural model is decoupled into two parts: A nonlinear one-dimensional beam model and a linear two-dimensional cross-section model. The blade dynamics model is shown in Fig. 1.

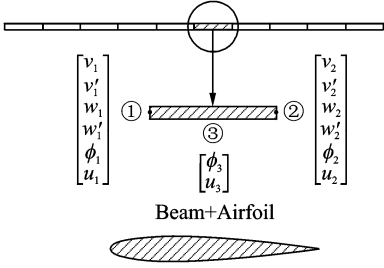


Fig. 1 Schematic of blade dynamics model

Each beam element includes two end nodes and one internal node at its midpoint. The end node has 6 degrees of freedom (DOFs): Axial displacement u_1/u_2 , transverse deflections v_1/v_2 , w_1/w_2 and their radial derivatives v'_1/v'_2 , w'_1/w'_2 , and torsional elastic deformation ϕ_1/ϕ_2 , while the internal node has only two DOFs (ϕ_3 and u_3).

Finite element modeling of the beam is based on Hamilton principle^[16]

$$\int_{t_1}^{t_2} (\delta U - \delta T - \delta W_e) dt = 0 \quad (5)$$

where U is the strain energy, T the kinematic energy and W_e the work of external loads, which are aerodynamic forces and moments of the blade in this analysis.

The strain energy, kinematic energy and work of external loads on the i th element can be derived from its degrees of freedom. The generalized displacements can be assumed as

$$\begin{bmatrix} \mathbf{v} \\ \mathbf{w} \\ \boldsymbol{\phi} \\ \mathbf{u} \end{bmatrix} = \begin{bmatrix} \boldsymbol{\Phi}_v^T & & & \\ & \boldsymbol{\Phi}_w^T & & \\ & & \boldsymbol{\Phi}_\phi^T & \\ & & & \boldsymbol{\Phi}_u^T \end{bmatrix} \begin{bmatrix} \mathbf{V} \\ \mathbf{W} \\ \boldsymbol{\Phi} \\ \mathbf{U} \end{bmatrix} \quad (6)$$

where \mathbf{v} , \mathbf{w} , $\boldsymbol{\phi}$, \mathbf{u} are generalized displacements at

any point on the beam element; $\boldsymbol{\Phi}_v$, $\boldsymbol{\Phi}_w$, $\boldsymbol{\Phi}_\phi$ and $\boldsymbol{\Phi}_u$ space-dependent interpolation functions; \mathbf{V} , \mathbf{W} , $\boldsymbol{\Phi}$ and \mathbf{U} time-dependent nodal parameters of each generalized displacement. Hermite interpolation polynomials are employed in space-dependent interpolation functions.

The finite-element equations of motion for the i th element are given by

$$\mathbf{M}_i \ddot{\mathbf{q}} + \mathbf{C}_i \dot{\mathbf{q}} + \mathbf{K}_i \mathbf{q} + \mathbf{F}_i = \mathbf{0} \quad (7)$$

where \mathbf{M}_i is the mass matrix, \mathbf{C}_i the damping matrix, \mathbf{K}_i the stiffness matrix, and \mathbf{F}_i the load vector. All the motion equations of each element are assembled and the nodal generalized displacement vector \mathbf{q} can be solved. More details on CSD model can be found in Ref. [16].

1.3 Rotor aerodynamic noise model

Rotor noise includes thickness noise, loading noise and quadrupole noise. When the blade tip speed is subsonic, the quadrupole noise is negligible. Based on F1A formula, rotor noise calculation is defined as

$$p'(\mathbf{x}, t) = p'_T(\mathbf{x}, t) + p'_L(\mathbf{x}, t) \quad (8)$$

where $p'(\mathbf{x}, t)$ is the total acoustic pressure, and $p'_T(\mathbf{x}, t)$ and $p'_L(\mathbf{x}, t)$ on the right hand side are thickness and loading noise pressure, respectively. Their expressions can be written as^[17]

$$4\pi p'_T(\mathbf{x}, t) = \int_{f=0} \left[\frac{-\rho_0 \dot{v}_n}{r(1-M_r)^2} \right]_{\text{ret}} dS + \int_{f=0} \left[\frac{\rho_0 v_n (r \dot{M}_i \hat{r}_i + c_0 M_r - c_0 M^2)}{r^2 (1-M_r)^3} \right]_{\text{ret}} dS \quad (9)$$

$$4\pi p'_L(\mathbf{x}, t) = \frac{1}{c_0} \int_{f=0} \left[\frac{\dot{l}_i \hat{r}_i}{r(1-M_r)^2} \right]_{\text{ret}} dS + \int_{f=0} \left[\frac{l_r - l_i M_i}{r^2 (1-M_r)^2} \right]_{\text{ret}} dS + \frac{1}{c_0} \int_{f=0} \left[\frac{l_r (r \dot{M}_i \hat{r}_i + c_0 M_r - c_0 M^2)}{r^2 (1-M_r)^3} \right]_{\text{ret}} dS \quad (10)$$

where the subscript *ret* denotes the retarded time. The terms appearing on the right of Eqs. (9), (10) are only related to surface integral and can be solved numerically using the airloads on the blade surface.

1.4 Flowchart of noise calculation based on CFD/CSD coupling method

The rigid body displacements of the blade can be easily obtained by Euler transformation. Besides, an efficient algebraic grid deformation

method^[18] is used to get blade elastic displacements. The deformation at arbitrary location on the blade can be defined as a function of radius and azimuth at the quarter chord and at any section, a rotation matrix \mathbf{T} and a vector \mathbf{x}_{in} are used to get the deformed grid coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \mathbf{T}^T \begin{bmatrix} x \\ y \\ z \end{bmatrix} + \mathbf{x}_{in} \quad (11)$$

where x , y and z are the grid coordinates before deformation.

Fig. 2 is the flowchart of noise calculation based on CFD/CSD coupling method. The detailed procedures are as follows.

(1) Generate a moving overset grid system

around the rotor;

(2) For the prescribed flight parameters and blade structural parameters, initialize the CSD module with a simple aerodynamic model;

(3) When the CSD solution is finished, the deformations of the blade are transferred to the CFD module;

(4) CFD time-marches at each azimuth (0.5 degrees per timestep);

(5) If the azimuth equals $360/N_b$ (N_b is the number of blades), the airloads are transferred to the CSD module.

Repeat steps (3–5) until the flowfield is converged. After that, rotor noise is calculated by F1A formula and the iteration is completed.

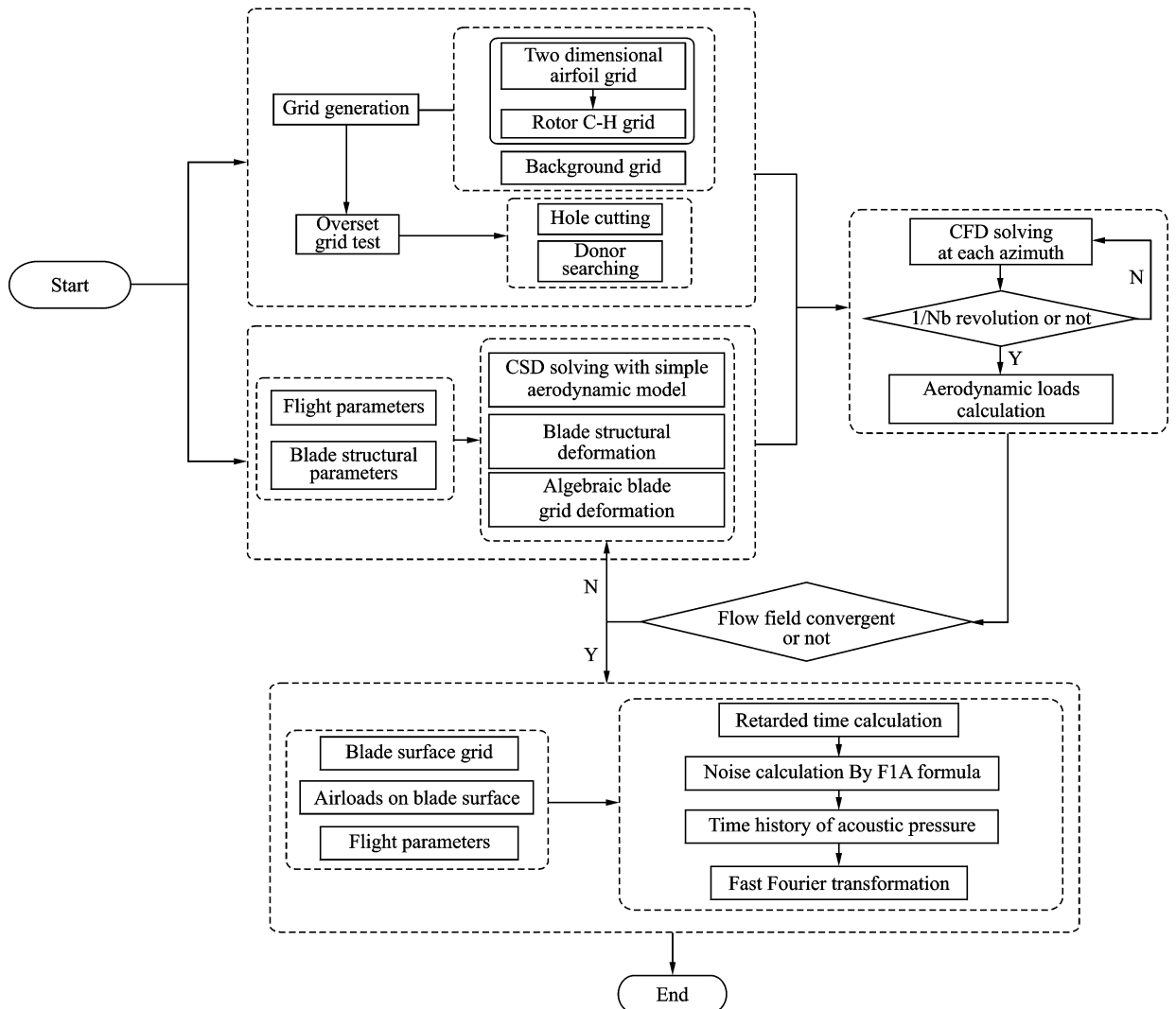


Fig. 2 Flowchart of noise prediction based on CFD/CSD coupling method

2 Validations of Numerical Methods

2.1 Validation of rotor CFD model

In order to verify the CFD model, the hovering UH-60A rotor case is presented firstly and the blade model is rigid in this section. The UH-60A is a four-bladed helicopter with advanced blade shape (multiple airfoils, variational chord and irregular twist)^[19]. Blade tip Mach number and collective pitch of the case are $Ma_{tip}=0.628$ and $\theta_{0.75}=9^\circ$. The blade grid follows a C-H topology. 198 points are used in the wrap around direction, 44 points in the normal direction, and 98 points in the spanwise direction. The schematic of the blade grid is given in Fig. 3. The background grid is Cartesian grid.

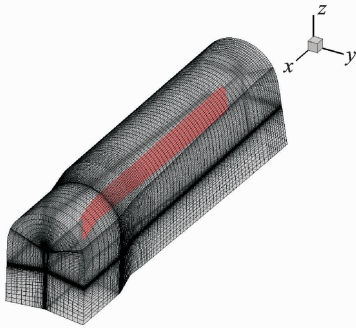


Fig. 3 Blade CFD grid used in simulations

The predicted blade pressure coefficients C_p from the CFD analysis are compared with test data in Ref. [20]. Two representative span stations are shown in Fig. 4.

From Fig. 4, it can be seen that the calculated C_p agrees favorably with the test data. The accuracy of the CFD model in this analysis is validated.

2.2 Validation of rotor CSD model

Nondimensional natural frequencies of the model rotor in Ref. [16] are calculated. The model rotor blade is isotropic, hingeless, and soft-in-plane. Frequency comparisons for the blade are summarized in Table 1. A blade-tip deflection analysis at $\mu=0.3$ is also conducted, and the comparisons with Ref. [16] are depicted in Fig. 5. It needs to be noted that in order to validate the CSD model solely, a quasi-steady aerodynamic

model is adopted in this section.

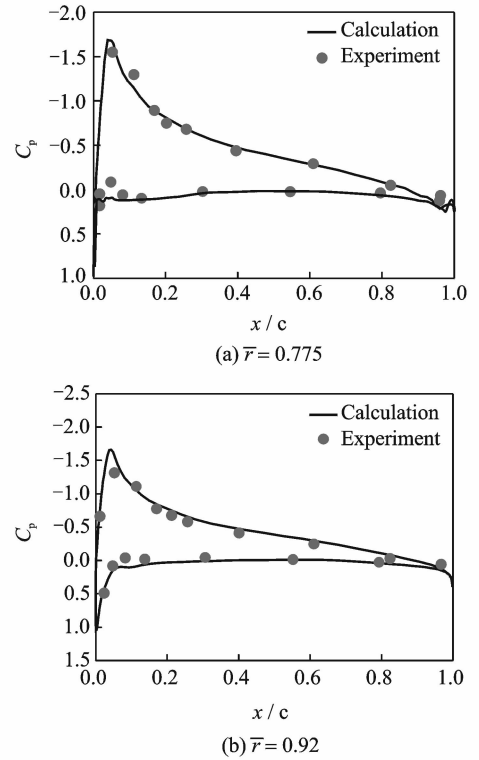


Fig. 4 Blade pressure coefficient of UH-60A in hover

Table 1 Natural frequencies of model rotor blade

Mode	Ref. [16]	Present
ω_{F1}	1.125	1.124 2
ω_{L1}	0.732	0.731 4
ω_{T1}	3.263	3.263 3

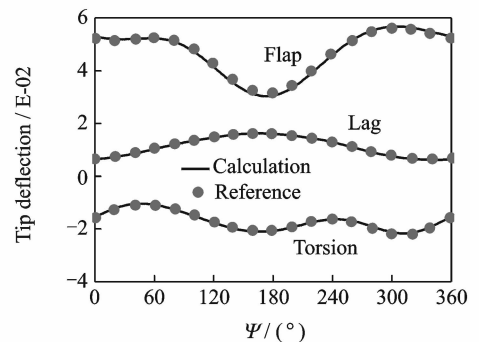


Fig. 5 Nondimensional blade-tip deflections of model rotor

As seen in Table 1 and Fig. 5, the calculated blade natural frequencies and tip deflections are highly correlated with the results in Ref. [16]. The availability of the CSD model is validated.

2.3 Validation of rotor noise model

The acoustic pressure time history result of

1/4 scale UH-1 model rotor at $\mu=0.2$ was compared with the data in Ref. [17]. The radius of this two-blade model rotor is 1.829 m and with a backward rotor shaft angle $\alpha_s=8.8^\circ$, and the coordinate of observation point is (3.21, -2.16, -0.3) m. As can be seen from Fig. 6, the acoustic pressure result of this paper has a favorable correlation with reference data.

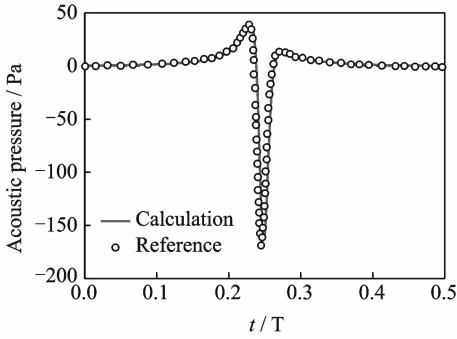


Fig. 6 Acoustic pressure of UH-1 model rotor

3 Airload and Noise Analysis Based on CFD/CSD Coupling

3.1 Rotor airload prediction based on CFD/CSD coupling

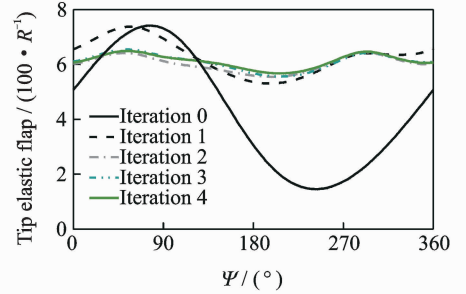
Airloads of flight test Counter C8513 of UH-60A isolated rotor in Ref. [21] are investigated to demonstrate the accuracy and robustness of CFD/CSD coupling model in this paper. C8513 is a low-speed level flight state. The flight parameters and trimmed control angles are documented in Table 2, and the azimuthal step size of CFD and CSD are 0.5° and 2° , respectively.

Table 2 Flight parameters of counter C8513

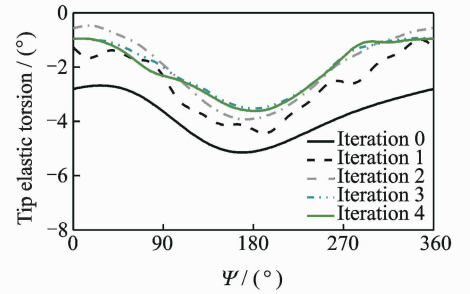
Item	Value
μ	0.153
C_T/σ	0.076
Ma_{tip}	0.644
Shaft angle/ $(^\circ)$	0.76
$\theta_{0.75}/(^\circ)$	6.0
$\theta_{1c}/(^\circ)$	3.1
$\theta_{1s}/(^\circ)$	-2.9

The elastic blade flap and torsion are considered very important to get correct prediction of airload. Since the effective angle of attack of each blade section is directly related to flap and torsion

variation. In Fig. 7, the elastic blade tip deflection results in flap and torsion of CFD/CSD coupling method are demonstrated. The coupling frequency between CFD and CSD is 90° and the solution has converged after 4 rotations of computation. As can be seen from the converged deflection curve, the mean elastic blade tip flap and torsion deflection of one rotation period are about $6\%R$ and -2° , respectively. Due to the high aspect ratio of UH-60A rotor blade, which approximately equals to 15.5, the influences of elastic blade flap and torsion on airload are significant even at a relative low advance ratio.



(a) Tip elastic flap



(b) Tip elastic torsion

Fig. 7 UH-60A blade tip elastic flap and torsion

Fig. 8 shows the vorticity iso-surfaces around the rotor based on CFD/CSD coupling. There are noticeable blade-vortex interactions at advancing and retreating side. Normal force coefficient comparisons with flight test data^[21] at three different sections are given in Fig. 9. Present isolated CFD method also calculates 4 rotations to obtain converged airload results. It can be seen that the rapid changes in blade airloads near 90° and 270° azimuths are captured for both the CFD method and the CFD/CSD coupling one, but the results from CFD method is overpredicted and less satisfactory than CFD/CSD method at the two outer sections. This can be mainly attributed to the inclusion of

flapwise and torsional elastic deflection in CFD/CSD coupling method. It is shown that the airloads calculated by CFD/CSD coupling method can be employed in the noise calculation.



Fig. 8 Vorticity iso-surfaces for UH-60A rotor

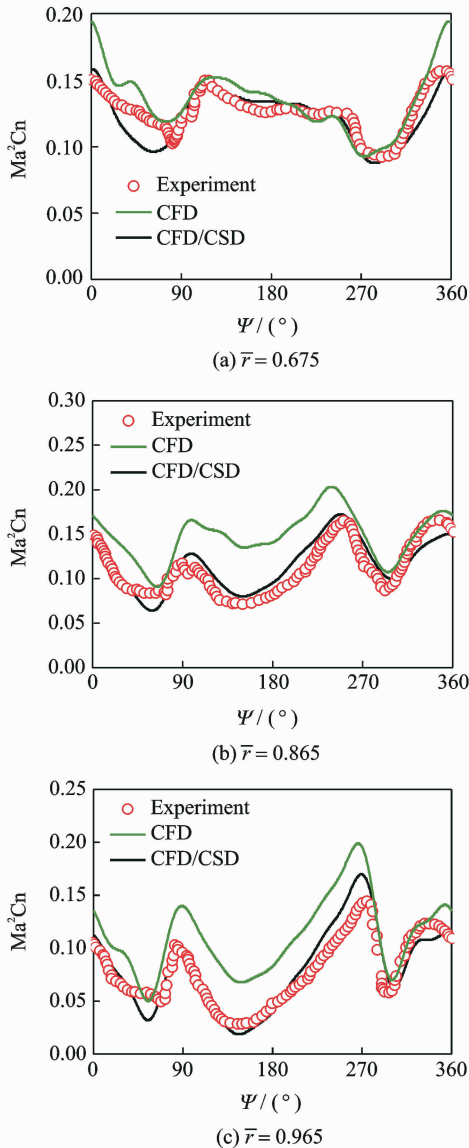


Fig. 9 Normal force coefficient for UH-60A rotor

3.2 Rotor noise prediction based on CFD/CSD coupling

One commonly used way to demonstrate the noise radiated from the rotor is to display the

magnitude and directivity on the surface of a noise hemisphere^[22]. Fig. 10 shows a typical noise hemisphere. The hemisphere is mapped to 2D plane by Lambert Conformal Conic projection and in this way one can get an intuitive understanding of noise radiation pattern.

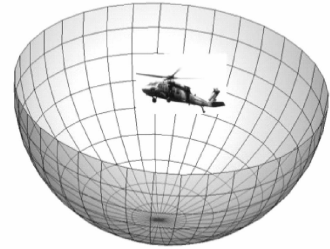


Fig. 10 Schematic of typical noise hemisphere

The noise hemisphere of flight test Counter C8513 of UH-60A is shown in Fig. 11. R_{obs} is the radius of noise hemisphere and let $R_{\text{obs}} = 3R$ in present analysis. The hemisphere is spread out along the 0° azimuth. The right side of the figure is the advancing side and the top of the projection is in front of the rotor. The center of the projection corresponds to the bottom of the hemisphere. Figs. 11 (a, b) represent thickness noise and loading noise distributions calculated by CFD/CSD method, respectively. Fig. 11 (c) is the difference of loading noise between CFD/CSD and CFD. It is needed to be noted that the effect of blade elastic deformation on thickness noise is negligible, thus the thickness noise calculated by isolated CFD method is not plotted.

It can be seen from Fig. 11 (a) that, in the rotor tip-path plane, thickness noise levels (above 95 dB) at 180° azimuth is higher than that at 0° and this phenomenon is caused by the Doppler effect. In addition, the noise level at the bottom of the rotor is much less than that in the rotor tip-path plane (below 40 dB). Therefore, the propagation of thickness noise is along the rotor tip-path plane.

As seen in Fig. 11 (b), when rotor operates in a BVI state and the transonic effect of blade tip is not significant, the loading noise is much higher than thickness noise and is the dominant source (above 100 dB at most observer positions). In

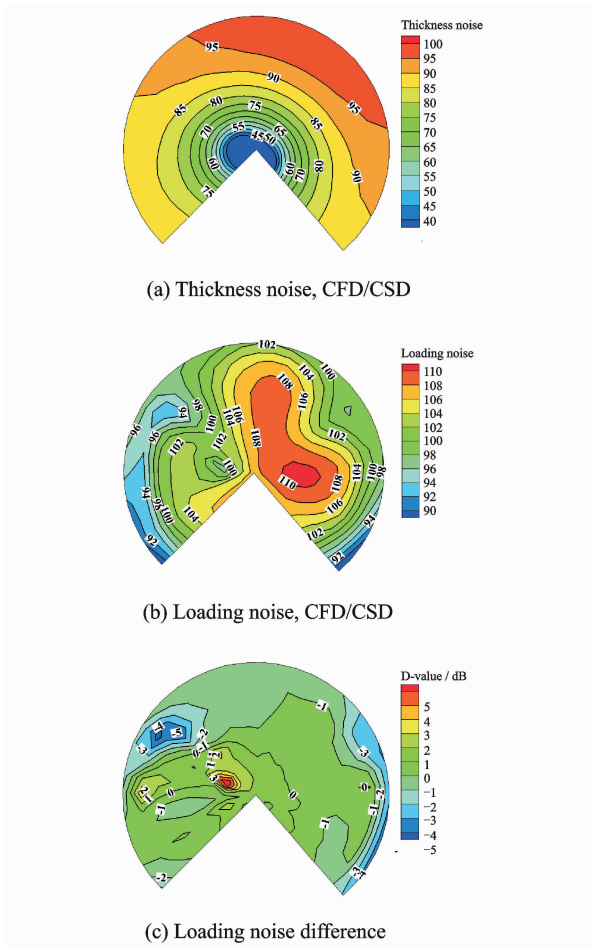


Fig. 11 Schematic of noise projection, $R_{\text{obs}} = 3R$

contrast with thickness noise, the "hotspot" of loading noise is approximately underneath the advancing side of the rotor.

Fig. 11 (c) shows that, for most observer positions on the hemisphere, there are only minor differences between the magnitudes of loading noise calculated by CFD/CSD and CFD. However, at some observer locations the difference of loading noise level can be up to 5 dB. This can be attributed to the different airloads calculated by the two methods. Thus a high fidelity in airloads prediction is necessary for accurate noise analysis.

The time and frequency domain results of peak thickness and loading noise are shown in Fig. 12 and Fig. 13, respectively. The noise spectrum is obtained by a Fourier analysis of acoustic pressure. Fig. 12 (a) demonstrates that thickness noise is characterized by periodic and negative pulses. Fig. 12 (b) illustrates that the amplitude

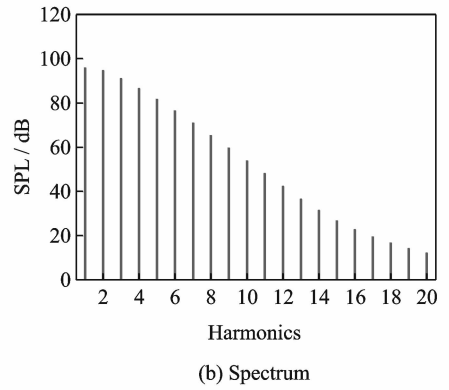
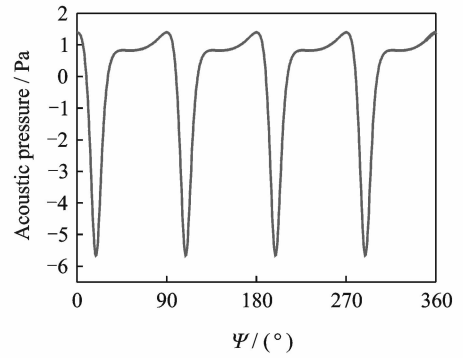


Fig. 12 Acoustic pressure and spectrum of peak thickness noise

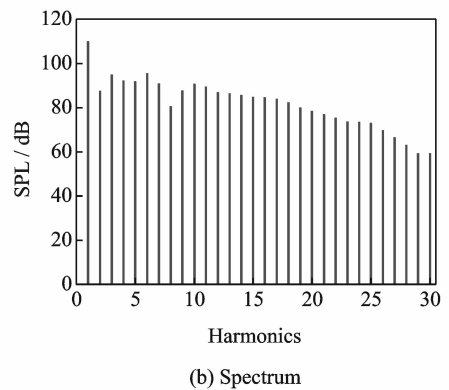
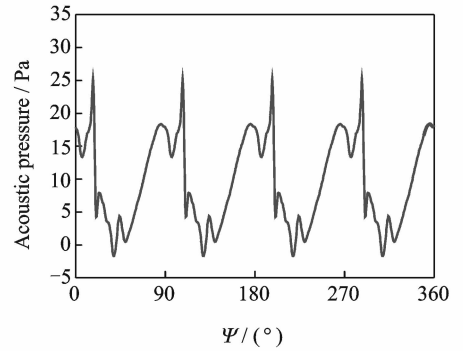


Fig. 13 Acoustic pressure and spectrum of peak loading noise

decreases rapidly with increasing harmonic number. As a contrast, the time history of loading noise in Fig. 13 (a) is not as smooth as Fig. 12 (a) and this is caused by the unsteady airloads. Besides, the harmonics fall off more slowly in Fig. 13 (b) than Fig. 12 (b).

4 Conclusions

A noise prediction method is developed with an implementation of CFD/CSD coupling. A low-speed forward flight case of UH-60A rotor is calculated and the airloads are used for rotor noise analysis. The following conclusions can be drawn from results presented:

(1) When the structural elasticity is taken into account, the difference of loading noise levels calculated by CFD/CSD and CFD can be up to 5 dB at some observer positions.

(2) For the low-speed forward flight state ($\mu=0.153$) investigated in this paper, there are blade-vortex interactions near 90° and 270° azimuths, which results in rapid fluctuations in blade airloads.

(3) The blade-vortex interactions are captured by both CFD/CSD method and isolated CFD method at three different sections calculated. However, the airloads predicted by isolated CFD method are less satisfactory than CFD/CSD coupling method.

(4) Loading noise level is much higher than thickness noise when rotor operates in a low tip Mach number and at a BVI condition, and it becomes the dominant contributor to rotor noise.

(5) A CFD/CSD coupling method for noise analysis is developed in this paper. Numerical examples show that the method is robust in flow-field simulation and noise prediction of rotors.

Acknowledgement

This work was supported by Funding of Jiangsu Innovation Program for Graduate Education (No. KYLX16_0389).

References:

[1] JOHNSON W. Helicopter theory[M]. New York,

USA: Dover Publications, 1994:10-11.

- [2] HUBBARD H H. Aeroacoustics of flight vehicles: Theory and practice NASA-AD-A241141 [R]. Hampton USA: National Aeronautics and Space Administration, 1991:102-105.
- [3] CONLISK A T. Modern helicopter rotor aerodynamics[J]. Progress in Aerospace Sciences, 2001,37(5): 419-476.
- [4] TUNG C, CARADONNA F X, JOHNSON W R. The prediction of transonic flows on an advancing rotor[J]. Journal of the American Helicopter Society, 1986,31(3):4-9.
- [5] POMIN H, WAGNER S. Navier-Stokes analysis of helicopter rotor aerodynamics in hover and forward flight[J]. Journal of Aircraft, 2002,39(5):813-821.
- [6] SITARAMAN J, ROGET B. Prediction of helicopter maneuver loads using a coupled CFD/CSD analysis [C]// 26th International Congress of the Aeronautical Sciences. Anchorage, Alaska, USA: The ICAS International Inc, 2008:1-26.
- [7] SMITH M J, LIM J W, van der Wall B G, et al. An assessment of CFD/CSD prediction state-of-the-art using the HART II international workshop data [C]// American Helicopter Society 68th Annual Forum. Fort Worth, USA: The AHS International Inc, 2012:1-41.
- [8] BOYD D D. HART-II acoustic predictions using a coupled CFD/CSD method[C]// American Helicopter Society 65th Annual Forum. Grapevine, Texas, USA: The AHS International Inc, 2009:1-19.
- [9] LIM J W, STRAWN R C. Prediction of HART II rotor BVI loading and wake system using CFD/CSD loose coupling [C]//Proceedings of the 45th AIAA Aerospace Sciences Meeting and Exhibit. Reno, Nevada, USA: AIAA, 2007:1-15.
- [10] WILLIAMS J E F, HAWKINGS D L. Sound generation by turbulence and surfaces in arbitrary motion [J]. Philosophical Transactions of the Royal Society of London A: Mathematical, Physical and Engineering Sciences, 1969,264(1151):321-342.
- [11] FARASSAT F. Derivation of formulations 1 and 1A of Farassat: NASA-TM-214853 [R]. Hampton, Virginia, USA: National Aeronautics and Space Administration, 2007:1-25.
- [12] WANG Junyi, ZHAO Qijun, XIAO Yu. Calculations on aeroelastic loads of rotor with advanced blade-tip based on CFD/CSD coupling method [J].

- Acta Aeronautica et Astronautica Sinica, 2014, 35 (9):2426-2437. (in Chinese)
- [13] XIAO Yu, XU Guohua, SHI Yongjie. Aeroelastic analysis of helicopter rotors using computational fluid dynamics/comprehensive analysis loose coupling model [J]. Proceedings of the Institution of Mechanical Engineers Part G Journal of Aerospace Engineering, 2014, 229(4):621-630.
- [14] SHI Yongjie, SU Dacheng, XU Guohua. Research on influence of shape parameters on blade-vortex interaction noise of helicopter rotor [J]. Journal of Nanjing University of Aeronautics and Astronautics, 2015, 47(2):235-242. (in Chinese)
- [15] BLAZEK J. Computational fluid dynamics: Principles and applications[M]. Kidlington, Oxford, UK: Elsevier, 2005:16-17.
- [16] YUAN K A, FRIEDMANN P P. Aeroelasticity and structural optimization of composite helicopter rotor blades with swept tips; NASA-CR-4665[R]. Hampton, Virginia, USA: National Aeronautics and Space Administration, 1995:106-107.
- [17] BRENTNER K S. Prediction of helicopter rotor discrete frequency noise: A computer program incorporating realistic blade motions and advanced acoustic formulation; NASA-TM-87721[R]. Hampton Virginia, USA: National Aeronautics and space Administration, 1986:1-93.
- [18] DATTA A, SITARAMAN J, CHOPRA I, et al. CFD/CSD prediction of rotor vibratory loads in high-speed flight[J]. Journal of Aircraft, 2006, 43(6): 1698-1709.
- [19] BOUSMAN W G. Aerodynamic characteristics of SC1095 and SC1094 R8 airfoils; NASA-TP-212265 [R]. Moffett Field, California, USA: National Aeronautics and Space Administration, 2003:1-50.
- [20] LORBER P, STAUTER R, Landgrebe A. A comprehensive hover test of the airloads and airflow of an extensively instrumented model helicopter rotor [C]// American Helicopter Society 45th Annual Forum. Boston, MA, USA: The AHS International Inc, 1989:1-16.
- [21] POTSDAM M, YEO H, JOHNSON W. Rotor airloads prediction using loose aerodynamic/structural coupling[J]. Journal of Aircraft, 2006, 43(3): 732-742.
- [22] GREENWOOD E. A physics-based approach to characterizing helicopter external noise radiation from ground-based noise measurements[D]. Maryland: Univ of Maryland, 2008.
- Mr. **Wang Liangquan** received his B. S. degree in aerospace science and engineering from Nanjing University of Aeronautics and Astronautics (NUAA), Nanjing, China, in 2013. He is currently a Ph. D candidate at National Key Laboratory of Science and Technology on Rotorcraft Aeromechanics of NUAA. His major research interests are helicopter aerodynamics and aeroacoustics, maneuvering flight simulation.
- Prof. **Xu Guohua** received his B. S. and Ph. D. degrees in aerospace science and engineering from NUAA in 1982 and 1996, respectively. From 1999 to 2000, he was a visiting scholar in University of Southampton, England. He is currently a full professor at National Key Laboratory of Science and Technology on Rotorcraft Aeromechanics of NUAA. His major research interests are focused on helicopter aerodynamics and aeroacoustics, rotor computational fluid dynamics.
- Dr. **Shi Yongjie** received his B. S. and Ph. D. degrees in aerospace science and engineering from NUAA in 2004 and 2010, respectively. He is currently an associate professor at NUAA. His major research interests are helicopter aerodynamics and aeroacoustics, rotor/fuselage interaction.

(Production Editor: Wang Jing)

