

# Reflection of Ultrasonic Wave on the Substrate-Ice Layer-Air Interface: The Role of Roughness Parameters

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(Received 5 November 2025; revised 16 January 2026; accepted 30 January 2026)

**Abstract:** Ice accretion on transmission lines poses a severe threat to the safety of power grids. To achieve early icing warning and online ice thickness measurement, it is necessary to consider the effect of the rough ice layer on ultrasonic echo signals during the early icing stage. This study applied a sinusoidal equivalent roughness model to simplify the ice layer profile, and used PZFlex to numerically analyze the effects of the rough structure scale on the ultrasonic pulse-echo signals. The reflection coefficient of the ice-air layer interface was introduced to characterize small-scale roughness. It is found that the attenuation of pulse-echo signals is dominant by the height of rough structure. As the roughness upper ice layer increases, the interface reflection coefficient gradually decreases. When the roughness exceeds the critical value, the reflection coefficient shows independent with roughness. As the threshold of reflection coefficient is set as 0.25, the effective measurement range of roughness under different center frequencies of excitation signal sources is determined. The relationship between the reflection coefficient and roughness upper ice layer is established, enabling the quantitative identification of rough ice layer using the ultrasonic pulse-echo technique. The research can provide a technical basis for the accurate measurement of ice thickness above transmission lines.

**Key words:** ice accretion on cables; ice roughness measurement; ultrasonic measurement technology; reflection coefficient

**CLC number:** TM75

**Document code:** A

**Article ID:** 1005-1120(2026)02-0275-11

## 0 Introduction

Ice accretion on overhead lines directly threatens the stability of power grids and induces issues such as grid overload<sup>[1]</sup>, line galloping<sup>[2]</sup>, tower inclination<sup>[3]</sup>, and insulator pollution flashover<sup>[4]</sup>, which severely endangers the safety of power systems. Traditional mechanical de-icing systems lack accurate operation instructions; therefore, ice monitoring on transmission lines is crucial for preventing grid freezing disasters.

Currently, the ice accretion state monitoring technologies for high-voltage transmission lines are

mainly categorized into the weighting method, tension-inclination method, optical fiber method, image method and simulated conductor method, etc<sup>[5]</sup>. Most of the aforementioned detection methods are based on the principle of electromagnetic measurement, which are susceptible to interference and unable to achieve long-distance online quantitative measurement of ice thickness or identification of ice types.

To improve the stability of online ice accretion monitoring for lines, ultrasonic detection is introduced for transmission lines icing. Previous studies

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**How to cite this article:** LU Qingwen, WANG Yuan, WANG Jingxin, et al. Reflection of ultrasonic wave on the substrate-ice layer-air interface: The role of roughness parameters[J]. Transactions of Nanjing University of Aeronautics and Astronautics, 2026, 43(2):275-285.

<http://dx.doi.org/10.16356/j.1005-1120.2026.02.008>

have demonstrated the feasibility of using ultrasonic waves to detect cable icing<sup>[6]</sup>. In 2023, Yang et al.<sup>[7]</sup> proposed a method for detecting the ice thickness of 10 kV overhead transmission lines using ultrasonic waves, with the relative error of the measured ice thickness being less than 10%. Liu et al.<sup>[8]</sup> proposed a method for direct ultrasonic detection of ice thickness on distribution lines using steel rods to simulate conductors, where the maximum error was less than 10%. However, the smooth surface of the simulated conductors fails to reflect the actual icing state.

The two aforementioned studies introduced ultrasonic detection technology for cable icing detection. However, for ultrasonic detection, the attenuation of echo signals is particularly pronounced when encountering different ice layer roughnesses. Therefore, identifying the surface roughness of ice deposits warrants special attention. To date, ice roughness measurement techniques are divided into contact and non-contact types. Traditional contact methods<sup>[9]</sup>, e.g., ice tracing and hot wax molding<sup>[10]</sup>, are inefficient, error-prone, and damage ice structures, leading to incomplete roughness data. Non-contact methods like close-range photogrammetry<sup>[11-13]</sup> or laser scanning<sup>[14-16]</sup> reconstruct ice profiles: The former uses multiple cameras but has large errors due to camera placement, glaze ice transparency and complex data processing; the latter is widely used for high-precision, multi-scale measurement<sup>[15]</sup> but requires developer due to optical properties of ice, leading to difficulty of real-time measurement.

In summary, current techniques struggle with initial icing stage and transient roughness measurement. Ultrasonic pulse-echo (UPE) technology shows advantages, which uses echo parameter changes to measure thickness and properties of ice<sup>[17]</sup>. Jr Hansman et al.<sup>[18]</sup> noted that ice surface properties affected ultrasonic signals, and Liu et al.<sup>[19]</sup> reported that frequency-dependent attenuation characterized glaze and rime ice. However, it is harder to measure ice surface roughness than ice thickness/density due to its spatiotemporal variations<sup>[20]</sup>. Relative research focus on the application of UPE on roughness surface measurement in other fields. Okajima et al.<sup>[21]</sup>

estimated planar Manning roughness coefficients using the peak-to-peak value of reflected ultrasonic pulses. Ma et al.<sup>[22]</sup> developed an ultrasonic reflection coefficient phase spectrum technique to measure coating interface roughness (6.2–12.7  $\mu\text{m}$ ). Hériveaux et al.<sup>[23]</sup> used a sinusoidal equivalent model to characterize bone-implant interface roughness via quantitative ultrasound. The results indicate that both of soft tissue thickness and interface roughness attenuate ultrasonic reflection coefficient. These studies confirm that surface roughness reduces ultrasonic interface reflection coefficients, which is beneficial to support UPE for measuring roughness upper ice layer of transmission lines.

Up to now, UPE technology has been initially applied in the field of aircraft icing<sup>[24]</sup>, but there have been no reports on its application in the icing monitoring of transmission lines, especially in the quantitative characterization of surface roughness. There is still a lack of detailed research on the influence of the roughness upper ice layers on the attenuation of ultrasonic signals.

Within the range of actual roughness ice on transmission lines, this study numerically analyzed the attenuation of echo signals caused by the rough structure between air-ice layer interface. Determining the attenuation of echo signals caused by roughness parameters provides a basis for selecting transducer frequency parameters in experimental measurements. Another approach involves simulating equivalent simplified real ice roughness to reduce experimental costs, thereby obtaining the relationship between a wide range of ice roughness values and ultrasonic echo parameters, which guides ultrasonic identification of ice surface roughness. This paper used a sinusoidal equivalent model to describe the ice layer shape. The change of surface roughness is adjusted by the amplitude height and period of the sinusoidal function. Ultrasonic echo signals under multi-frequency excitation signals and different surface roughness are obtained through numerical simulation. The reflection coefficient affected by the ice layer shape is introduced to characterize ice roughness at different scales. The relationship between the effective identification range of roughness upper

ice layer and the frequency of the excitation signal is established.

## 1 Methods and Theories

### 1.1 Establishment of a simulation model for ice layers

As a powerful professional tool in acoustics, PZFlex software is specifically developed for piezoelectric and ultrasonic applications. The software adopts an explicit finite element algorithm, which is suitable for simulating piezoelectricity, ultrasonic wave propagation, and long-range wave propagation.

To study the influence of roughness at different scales on the attenuation of ultrasonic pulse-echo signals, the models and simulations of roughness ice are solved via PZFlex in this paper. The actual physical model is a complex-shaped cable with accreted ice. However, due to the small size of the applied transducer and the single-point measurement of the ice layer above its geometric center, the numerical model can be simplified to a 2D axisymmetric model. The process mainly involves model construction, mesh generation, material parameter configuration, and boundary conditions.

Due to the symmetry, a 2D axisymmetric model is used to reduce computational load. The model includes four parts: Pressure loading area, aluminum substrate, ice layer, and roughness. A non-structured mesh is used, with grid refinement for the ice layer interior; the rest adopts a 20  $\mu\text{m}$  per grid, satisfying the requirement of at least 15 grids per wavelength. The upper surface of ice layer is set as a total reflection interface, while other boundaries are total absorption interfaces to reduce oscillation interference from secondary interface echoes. In the study, the transducer has a diameter of 6 mm. As the width of the load application area should be smaller than the model width, the width of both ice layer and substrate is set as 15 mm. The thickness of substrate, ice layer and load application area are 5, 1.6 and 0.5 mm, respectively. The rough profile on the ice surface is implemented via a sinusoidal function, with a single roughness element illustrated

in the local enlarged view of Fig.1, where  $S_0$ ,  $S_1$  and  $S_2$  represent the regions areas. The curve expression of roughness is expressed as

$$y = A \cdot \sin\left(\frac{2\pi}{T}x\right) \quad (1)$$

where  $A$  is the amplitude and  $T$  the period.

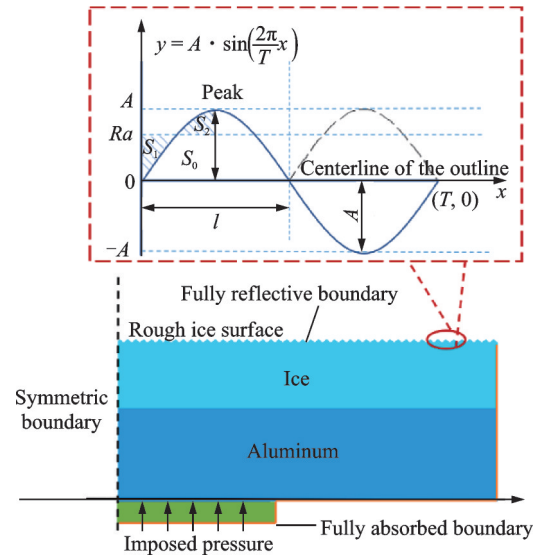


Fig.1 Schematic diagram of a simplified 2D symmetric finite element model for rough ice surfaces

The sinusoidal function is mainly described by two parameters: Amplitude  $A$  and period  $T$ . Roughness  $Ra$  is the arithmetic mean of the absolute values of profile deviations within the sampling length. Therefore, the roughness formula for this model is calculated as

$$Ra = \frac{1}{l} \int_0^l A \cdot \sin\left(\frac{2\pi}{T}x\right) dx \quad (2)$$

For  $l = T/2$ , the calculated roughness  $Ra$  is expressed as

$$Ra = \frac{1}{l} \cdot \frac{AT}{\pi} = \frac{2A}{\pi} \quad (3)$$

According to above derivation, the average roughness  $Ra$  can be adjusted only by changing the peak value  $A$  in the sinusoidal function. Additionally, in all numerical cases, the average height of the surface roughness is regarded as the origin of the  $y$ -axis. It is assumed that all media have uniform and isotropic mechanical properties. The substrate material is 7075 aluminum alloy. The material properties<sup>[25-26]</sup> used in the simulation, with references, are presented in Table 1.

**Table 1** Material attribute

Material	Mass density $R/(\text{kg}\cdot\text{m}^{-3})$	Longitudinal velocity $v_p/$ $(\text{m}\cdot\text{s}^{-1})$	Shear velocity $v_s/(\text{m}\cdot\text{s}^{-1})$
Ice	900	3 900	2 120
Aluminum	2 690	6 306	3 114

## 1.2 Finite element simulation

Dynamic equations were solved in the time domain via the PZFlex software. Post model construction and material assignment, the loading excitation signal were configured, and mesh generation was conducted. A Ricker wavelet served as the ultrasonic pulse excitation source.

To explore frequency-dependent roughness measurement ability, the simulation included excitation signals with center frequencies ( $f_c$ ) of 3.2, 5.3, 7.5, 10, 12.8, and 15.5 MHz. During model establishment, the grid size is first determined by the signal's center frequency. A non-structured mesh is adopted, with a requirement of at least 15 elements per wavelength in the material. For grid size in the ice layer, the maximum center frequency is used to calculate the minimum wavelength, with the formula given below

$$\lambda_{\min} = v_p / f_c \quad (4)$$

To explore the roughness-dependent echo signal, the roughness parameter was varied within the range of 0—1 000  $\mu\text{m}$  in the study. For grid independence verification, the roughness size and the center frequency were fixed at 25  $\mu\text{m}$  and 10 MHz, respectively. The grid size was evenly varied within the range of 1—10  $\mu\text{m}$ . The verification results are presented in Fig.2 and Fig.3. The results indicate that when the grid size exceeds 5  $\mu\text{m}$ , both the amplitude and phase of the echo signal are unstable. To ensure clarity, only echo signals for grid sizes of 1—5  $\mu\text{m}$  are presented in Fig.2. Observing the ice layer echo signals, the amplitude fluctuation of the echo peak is below 1% when the grid size is smaller than 4  $\mu\text{m}$ , indicating that the echo peak at the air-ice interface is stable. Fig.3 presents the phase errors between the air-ice interface echo, substrate-ice interface echo, and the set thickness within the range of

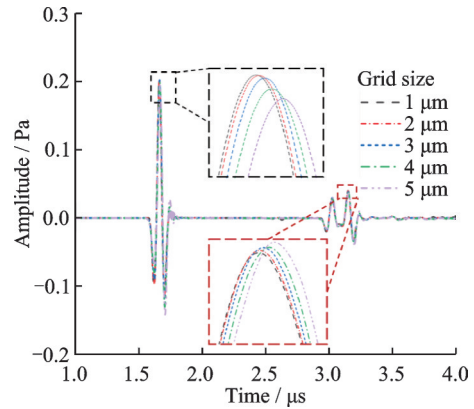


Fig.2 Variations in echo signals from the upper surface of the ice layer corresponding to different grid sizes

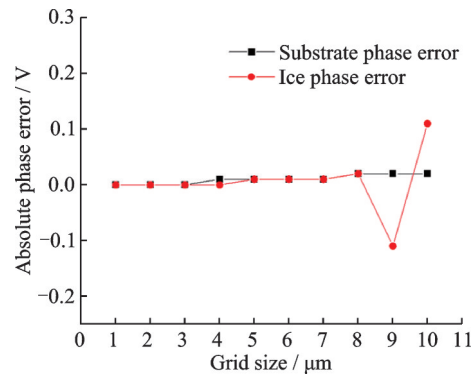


Fig.3 Phase deviation between rough ice layer height and original height corresponding to different grid sizes

1—10  $\mu\text{m}$ . The results show that the peak time of the interface echo stabilizes when the grid size is below 3  $\mu\text{m}$ . Considering the grid size for stability of echo signals, the grid size is set as 3  $\mu\text{m}$ , to save computing loads and ensure the accuracy of numerical calculation results.

An un-structured rectangular mesh was adopted to reduce the number of meshes. For time-domain calculations, the maximum stable time step was set based on the minimum mesh size, as follows

$$\Delta t_{\max} = d_{\min} / c_p \quad (5)$$

where  $d_{\min}$  denotes the minimum mesh side length, and  $c_p$  the maximum longitudinal wave speed in the model material.

The maximum stable time step is multiplied by a safety factor  $k_0 = 0.8$  to obtain the maximum simulation timestep. Thus, the actual timestep  $t_s$  used in the simulation is given by

$$t_s = k_0 \cdot \Delta t_{\max} = 0.38 \times 10^{-9} (\text{s}) \quad (6)$$

Signal acquisition frequency is

$$f_0 = \frac{1}{t_s} \quad (7)$$

The sampling frequency meets the requirement of being greater than 10 times the center frequency. The simulation time is determined based on the transit time of the multi-layer material thickness, and is ultimately set to 5  $\mu$ s through calculations.

From the derived formula for roughness, it can be seen that this expression is determined solely by the amplitude  $A$ . However, based on the inferred physical propagation of acoustic waves, variations in the period parameter  $T$  also induce changes in the model and consequently affect the echo signal. Therefore, the parameter  $B = T/A$  was defined. With the amplitude  $A$  kept constant, simulations were conducted to investigate the effect of period  $T$  on the reflection coefficient of ultrasonic echo signals by varying period. The results are presented in Fig.4.

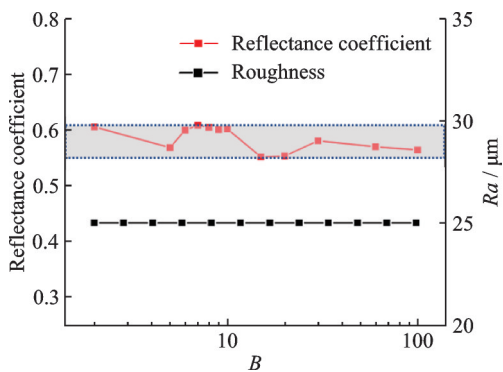


Fig.4 Effect of period variation of the sinusoidal function on roughness and reflection coefficient

Parameter  $B$  was assigned non-uniform values within the range of 0—100. It can be observed that parameter  $B$  exerts a certain influence on the echo signal. When  $B > 10$ , the rough profile curve tends to approach a straight line, regraded as smooth surfaces. When  $B < 10$ , variations in the period cause a relative error of 3% in the reflection coefficient. However, in actual measurements, ultrasonic detection acquires the average value of reflected echoes from the rough surface within the ice layer surface detection range. Thus, the influence of the period parameter is minimal. Furthermore, there is no need to decouple the effects of the period and ampli-

tude on the echo characteristic parameters. In subsequent simulation cases, the period was set to  $T = 2A$ , and the roughness value in the simulation was adjusted solely by varying the amplitude parameter. The settings of the ice layer roughness parameters are presented in Table 2.

**Table 2 Settings for roughness in the simulation model**

Serial number	Amplitude $A/m$	Cycle $T$	Roughness $Ra/\mu m$
1	0.00E+00	1.00E-03	0
2	3.93E-05	7.86E-05	25
3	7.85E-05	1.57E-04	50
4	1.18E-04	2.36E-04	75
5	1.57E-04	3.14E-04	100
6	2.36E-04	4.72E-04	150
7	3.14E-04	6.28E-04	200
8	3.93E-04	7.86E-04	250
9	4.71E-04	9.42E-04	300
10	5.5E-04	1.10E-03	350
11	6.29E-04	1.26E-03	400
12	7.07E-04	1.41E-03	450
13	7.85E-04	1.57E-03	500
14	8.64E-04	1.73E-03	550
15	9.43E-04	1.89E-03	600
16	1.10E-04	2.20E-03	700
17	1.26E-04	2.51E-03	800
18	1.41E-04	2.83E-03	900
19	1.57E-04	3.14E-03	1 000

### 1.3 Signal processing

In this study, ultrasonic echo signals from multi-layer medium interfaces with/without roughness were obtained via simulation calculations. The signals in the time domain were recorded and subsequently processed using MATLAB software. First, the Hilbert transform is applied to the echo signals, and the transformation results are presented in Fig.5. The solid line represents the original signal, while the dashed line denotes the signal envelope. Two gates #1 and #2 are set; Gate #1 covers the complete echo signal from the substrate-ice interface, while Gate #2 covers the complete echo signal from the ice-air interface. After envelope processing, the echo amplitudes  $p_{A-1}$  (substrate-ice interface) and  $p'_{A-1}$  (ice-air interface), along with their corresponding peak time  $t_1$  and  $t_i$ , are identified with-

in the two gates, respectively. The real-time ice layer thickness is calculated using  $t_1$  and  $t_i$  based on the ultrasonic transit time in the structure, which is used to compute ultrasonic attenuation in the ice. The substrate-ice interface echo amplitude  $p_{A-1}$  is acquired. The echo amplitude  $p_{I-a}$  for the ice-air interface with a smooth surface is calculated theoretically and numerically. In addition, under the same ice layer thickness, this study obtains the ice-air interface echo amplitude  $p'_{I-a}$  when small-scale roughness elements exist on the ice surface. The formula for the ultrasonic reflection coefficient  $R'_{I-a}$  at the ice-air interface with a rough structure is as follows

$$R'_{I-a} = \frac{p'_{I-a}}{p_{I-a}} \quad (8)$$

A comparison of simulation results between smooth ice surfaces and ice surfaces with rough profiles reveals that the waveform and phase of the echo signal at the substrate-ice interface are both affected by ice surface roughness. From the signal comparison in Fig.5, it is evident that when small-scale roughness elements exist on the ice surface, the echo amplitude at the ice-air interface decreases significantly, accompanied by phase delay. This conclusion is further confirmed by observing the shift in the peak points of the envelope. Thus, it is feasible to characterize the influence of roughness on ultrasonic echo signal by using the reflection coefficients.

Fig.6 illustrates the entire process of extracting characteristic parameters of ultrasonic echo signals. First, after determining the simulation model,

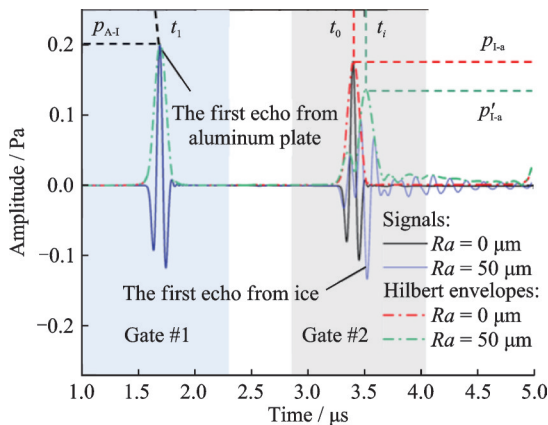


Fig.5 Schematic diagram of ultrasonic echo signal feature parameter extraction

roughness parameters are input. The reflection coefficient is then obtained by applying the aforementioned signal processing method and extracting amplitude parameters via envelope processing. By processing the original ultrasonic pulse-echo signals, the ultrasonic reflection coefficient at the ice-air interface was obtained. A corresponding relationship can be established between the reflection coefficient  $R'_{I-a}$  and roughness parameters  $Ra$ . Therefore, the reflection coefficient can be used to calculate and predict the surface roughness of the ice layer.

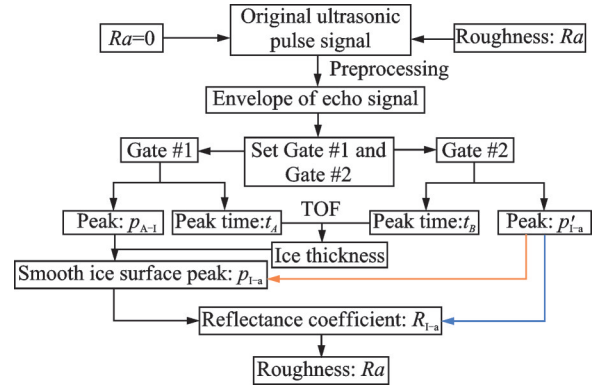


Fig.6 Flowchart for extraction of ultrasonic echo signal characteristic parameters

## 2 Results

### 2.1 Effect of surface roughness on ultrasonic signals

A series of numerical simulations were performed using the roughness parameters listed in Table 2. Glaze ice was selected as the representative ice type for simulations due to its hazard. The ultrasonic attenuation coefficient inside the simulated ice layer was set to  $0.05 \text{ Np} \cdot \text{mm}^{-1}$ . The theoretical ice density was  $\rho_{(i)} = 900 \text{ kg} \cdot \text{m}^{-3}$ , and the longitudinal wave speed was set to  $3900 \text{ m} \cdot \text{s}^{-1}$ . In a homogeneous solid, longitudinal waves propagate in a straight line with relatively low energy loss, producing a clear “emission-bottom echo” signal.

The original echo signals undergo preprocessing. After that, the ultrasonic echo envelopes, under different roughness conditions, are shown in Fig.7. The results show that with the increase of ice-air interface roughness, the echo amplitude decreases

es irregularly and the arrival time of the peak shifts progressively later. For a perfectly smooth ice surface ( $Ra = 0$ ), the echo amplitude at the ice-air interface was  $p_{1a} = 0.85$ .

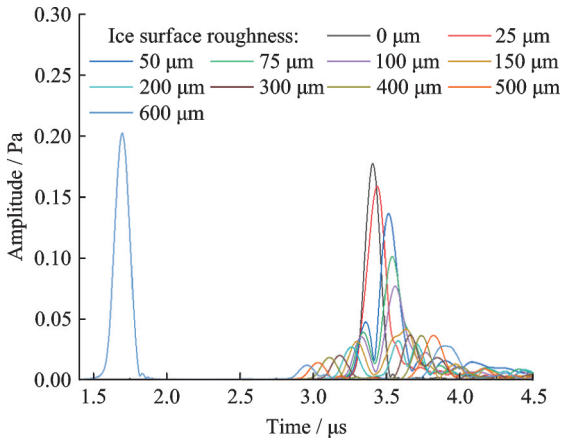


Fig.7 Influence of roughness on echo signals envelopes

Using the feature-extraction method described in Fig.6, the ultrasonic reflection coefficient of the ice-air interface was determined as a function of surface roughness, as shown in Fig.8. The simulation was performed at a center frequency of 7.5 MHz. The resulting curve agrees well with previously published results on effect of surface roughness<sup>[24]</sup>.

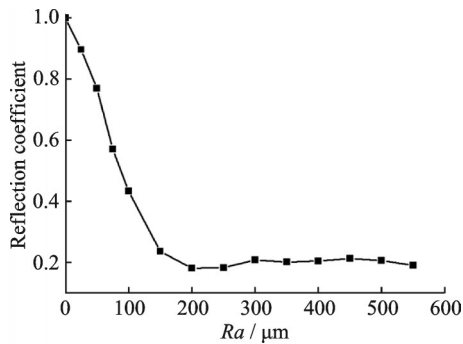


Fig.8 Reflection coefficient versus surface roughness

From Fig.8, when the surface roughness increases from 0 to 150  $\mu\text{m}$ , the interface reflection coefficient  $R'_{1a}$  decreases from 1 to 0.23. For roughness values exceeding 150  $\mu\text{m}$ ,  $R'_{1a}$  stabilizes at about 0.2, showing a slight rise followed by a further decline. This behavior occurs because the sinusoidal roughness profile has alternating peaks and valleys. When the roughness becomes sufficiently large, the ultrasonic wave can resolve the height dif-

ference between the peaks and valleys, causing the ice-air interface echo to split into two distinct signals. Consequently, the reflection coefficient derived from the envelope analysis shows a slight increase before continuing to decline as roughness grows. For example, at a center frequency of 7.5 MHz, when the roughness is in the range of 0 — 100  $\mu\text{m}$ , the echo signals are aliasing; once the roughness exceeds 100  $\mu\text{m}$ , the echo signals become separated. The reflection coefficient decreases by as much as 80%, demonstrating that the ultrasonic reflection coefficient  $R'_{1a}$  is highly sensitive to roughness variations. Furthermore, the accuracy of using  $R'_{1a}$  as a quantitative indicator of surface roughness is confirmed.

## 2.2 Influence of center frequency on rough-surface echoes

The sensitivity of ultrasonic roughness detection varies with center frequency. To examine this effect under constant ice-layer thickness, the surface roughness was fixed at 100  $\mu\text{m}$  while the center frequency of the ultrasonic excitation source was varied. The corresponding ice-air interface echo signals are shown in Fig.9. A higher excitation signal frequency results in a narrower bandwidth, higher detection sensitivity, and greater signal attenuation. Simulation results show that as the center frequency increases, the amplitude of the echo signal at the rough ice-air interface decreases monotonically. Furthermore, applying a high-frequency excitation source, two complete echo signals can be obtained, corresponding to the peak and trough points of the rough profile, respectively. This leads to greater attenuation of the high-frequency excitation signal under the same ice thickness and roughness conditions.

For ultrasonic pulse-echo detection signals with different center frequencies, there are significant differences in the identifiable scale range of material surface rough structures due to variations in their inherent wavelengths, attenuation coefficients, and detection sensitivity characteristics. High-frequency signals are more capable of identifying small-scale roughness values but suffer from greater energy at-

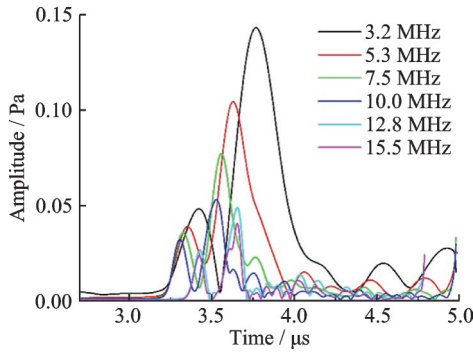


Fig.9 Effect of frequency variation on ultrasonic echoes from a rough ice surface

tenuation. However, low-frequency signals are suitable for larger-scale rough structures. These differences directly affect the measurement range and accuracy of rough features. To further investigate the capability of the ultrasonic pulse-echo technique for quantitative measurement of wide-range roughness, physical property measurements of ice layers with rough profiles were conducted under different center frequencies. The resulting reflection coefficients are presented in Fig.10. When  $Ra = 50 \mu\text{m}$ , the reflection coefficient decreases monotonically as the center frequency increases. When  $Ra$  increases to  $200 \mu\text{m}$ , the reflection coefficient shows significant decrease once center frequencies exceeds 5.3 MHz. After the reflection coefficient falls below 0.25, interface echoes in the original signal waveform exhibit aliasing and low amplitude, making it impossible to distinguish from clutter. With a further increase in roughness size, the reflection coefficient shows no obvious change, and direct identification of roughness parameters via interface echo signals becomes infeasible in the situations.

The detection range of roughness measurement

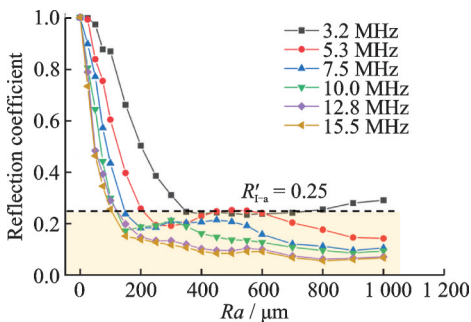


Fig.10 Ultrasonic reflection coefficient of the ice-air interface versus roughness

for different frequencies is shown in Fig.11.

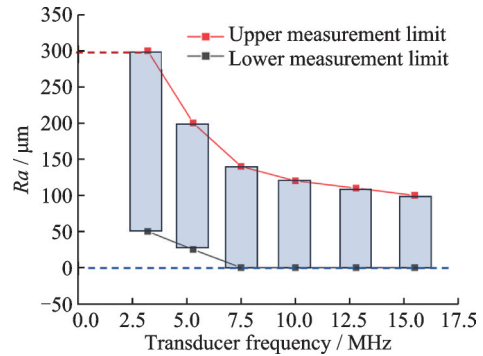


Fig.11 Roughness measurement range at different frequencies

In this study, a critical threshold of  $R'_{ra} = 0.25$  was used to distinguish the effective center frequency. As the center frequency increases, the upper limit of effective roughness identification decreases, while the accuracy of identifying small-scale roughness improves. The results show that as the transducer frequency increases, the upper limit of roughness measurement generally shows a decreasing trend. Meanwhile, the lower limit of roughness measurement gradually approaches 0 and stabilizes as the frequency increases. The result indicates that high-frequency transducers possess the capability to identify smaller-scale surface roughness features.

The higher the transducer frequency, the lower the upper limit of surface roughness can be accurately measured, while the stronger the ability to identify smaller rough structures. To quantitatively analyze the roughness identification range for different frequencies  $f$ , the fitted formula is as follows

$$Ra_{max} = 607 \exp(-f/2.9) + 99.36 \quad (9)$$

$$Ra_{min} = \begin{cases} -11.63f + 87 & f \leq 7.5 \\ 0 & f > 7.5 \end{cases} \quad (10)$$

The influence laws of frequency and roughness on the ultrasonic reflection coefficient at the ice-air interface were refined via simulation calculations. The ice surface roughness range was determined. Then, the center frequency of the excitation source was selected. After extracting the characteristic parameters of the original signals, the corresponding relationship was obtained as shown in Fig.12.

The results in Fig.12 show that there is a

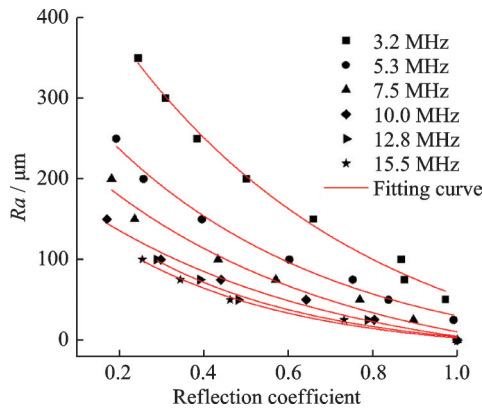


Fig.12 Relationship between ultrasonic reflection coefficient and roughness at the ice-air interface

monotonic relationship between roughness and reflection coefficient within a certain range. The red solid lines represent the fitting curves of roughness and ultrasonic reflection coefficient under different frequencies. The formula of the fitting curve is as follows

$$Ra = a_1 \cdot \exp(-R'_{1a}/a_2) + a_3 \quad (11)$$

where  $a_1$ ,  $a_2$  and  $a_3$  are the coefficients of the equation, and their variation relationships are expressed in Table 2.

**Table 3** Equation coefficients

Frequency/MHz	$a_1$	$a_2$	$a_3$
3.2	603.7	0.59	-56.5
5.3	387.7	0.537	-30.3
7.5	319.3	0.592	-48.7
10.0	248.7	0.595	-41.88
12.8	232.6	0.413	-16.68
15.5	212.2	0.415	-16.48

The ultrasonic reflection coefficient  $R'_{1a}$  varies within the range of 0.2 — 1, corresponding to a roughness measurement range of 0 — 300  $\mu\text{m}$ .

### 3 Conclusions

To investigate the reflection of ultrasonic echo signals on the substrate-ice layer-air interface, a novel multilayer model with a sinusoidal profile was introduced to simulate ultrasonic reflections from the roughness shape upper the ice layer. By adjusting the amplitude and period of the sinusoidal function, the available measure ranges of roughness ice surface at different center frequencies are quantitatively analyzed. The main findings are as follows.

(1) With the same center frequency, as the surface roughness increases, the amplitude of echo signals decreases and the phase of the peak point delays. The interface reflection coefficient gradually decreases until it shows independent of roughness and reflection coefficient.

(2) For small-scale roughness, as the center frequency increases, the both of the echo signal amplitude and the reflection coefficient also decrease monotonically. For large-scale roughness, increasing the center frequency leads to a significant decline in the reflection coefficient until it shows independent of the roughness and center frequency.

(3) As the center frequency increases, the upper limit for identifying effective roughness decreases, while the accuracy in identifying small-scale roughness increases.

(4) The reflection coefficient threshold is set as 0.25, the ice surface roughness value is quantitatively characterized through the interface echo signal, and the calculation formulas for roughness is fitted for various center frequency.

Applying ultra-pulse echo technology to monitor the transient icing process of transmission lines, it is important to select an appropriate transducer frequency for ice layers with different roughness to maximize the monitoring range. The research can provide a technical basis for the accurate measurement of ice thickness on transmission lines.

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**Author contributions** Miss. LU Qingwen was responsible for drafting the core content and proofreading the manuscript to ensure textual accuracy and standardization. Dr. WANG Yuan assisted in organizing the research framework and selecting methodologies, participating in specialized discussions. Dr. WANG Jingxin and Dr. WANG Yan reviewed the article content, conducting scientific validation and verification to ensure the reliability of the findings. Prof. ZHU Chunling and Prof. ZHU Chengxiang provided research funding support. Mr. LI Bin and Mr. REN Zhanpeng managed the related project, coordinating resources and progress. All authors commented on the manuscript draft and approved the submission.

**Competing interests** The authors declare no competing interests.

(Production Editor: ZHANG Huangqun)

## 基底-冰层-空气界面超声波反射:粗糙度参数的作用

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**摘要:** 输电线路结冰对电网安全构成严重威胁。为实现冰冻早期预警与在线冰厚测量, 需考虑结冰初期粗糙冰层对超声回波信号的影响。本文采用正弦等效粗糙度模型简化冰层截面, 运用PZFlex软件研究不同粗糙结构尺度对超声脉冲回波信号的影响。引入冰层-空气界面反射系数表征小尺度粗糙度。研究发现脉冲回波信号衰减主要受粗糙结构高度主导: 随着冰层表面粗糙度增大, 界面反射系数逐渐降低; 当粗糙度超过临界值时, 反射系数与粗糙度呈现无关性。以反射系数阈值0.25为基准, 确定了不同中心频率激励信号下粗糙度的有效测量范围。建立了反射系数与粗糙冰层的关联, 实现了利用超声脉冲回波技术对粗糙冰层进行定量识别。该研究为输电线路冰厚精确测量提供了技术依据。

**关键词:** 线缆结冰; 冰粗糙度测量; 超声测量技术; 反射系数

**研究亮点:**

1. 引入超声换能器应用于线缆覆冰监测, 通过仿真考虑冰表面粗糙度建立中心频率适用范围。
2. 提出了基于界面声波反射系数定量表征冰层表面粗糙度方法。