

# Structure Design of Shaped Charge for Requirements of Concrete Crater Diameter

Guo Jian(郭坚), He Yong(何勇)\*, Xiao Qiangqiang(肖强强),  
Huang Zhengxiang(黄正祥), Liu Beibei(刘蓓蓓)

School of Mechanical Engineering, Nanjing University of Science and Technology, Nanjing 210094, P. R. China

(Received 18 November 2014; revised 2 January 2015; accepted 12 March 2015)

**Abstract:** When shaped charge penetrates into concrete, crater diameter must meet certain requirements. By using theories of shaped jet formation and crater diameter growth during jet penetrating concrete, we revealed the thresholds of the velocity and diameter of jet head, and therefore obtained the related structure parameters of top liner, so that shaped charge structure was developed. We built a  $\varnothing 60$  mm copper liner and a  $\varnothing 142$  mm Ti-alloy liner which followed the rules of 0.6 cal and 0.7 cal in-crater diameter, respectively. X-ray experiment and penetration test results showed that the parameters of jet head were consistent with the results of theoretical analysis. The in-crater diameter of  $\varnothing 60$  mm shaped charge reached 36 mm, and the  $\varnothing 142$  mm one reached 100 mm. They both met the design requirements.

**Key words:** shaped charge; crater diameter; structure design

**CLC number:** TJ410.2

**Document code:** A

**Article ID:** 1005-1120(2015)06-0681-06

## 0 Introduction

As the application area of shaped charge is expanding to some special fields, including precursory charge of tandem warhead<sup>[1]</sup>, and petroleum perforation bullet<sup>[2]</sup>, other than shaped charge penetration depth requirements, additional condition that penetration crater diameter must be as large as possible is also demanded. Enlarging penetration crater diameters can increase damage power of shaped charge.

Many scholars at home and abroad have focused on structural design and optimization for shaped charge to increase jet penetrating crater diameter. Huerta et al.<sup>[3]</sup> used numerical simulation to structurally design and optimize single cone shaped charge and verified it by experiments. Xiao et al.<sup>[4]</sup> designed double material composite of jet shaped charge to increase crater diameter. Zhou Quan<sup>[5]</sup> conducted multi-objective optimization design based on orthogonal test to

reach two objectives of penetration depth and crater diameter, and the latter was selected as the main objective function. Ma Jianfu<sup>[6]</sup> investigated the influence of structure and materials of shaped charge on penetration depth and crater diameter in the process of jet penetration.

We developed a structure of top liner to increase crater diameter based on the theory of shaped jet formation and crater diameter growth theory during jet penetration. Then we designed shaped charge structure and tested it. The experiments verified that the method could be applied to structure design of large crater diameter shaped charge.

## 1 Theoretical Analysis

### 1.1 Structure design

Szendrei/Held equations provided the relationship between penetration crater diameter and velocity & diameter of shaped charge jet<sup>[7-11]</sup>

\* **Corresponding author:** He Yong, Professor, E-mail: yhe1964@njust.edu.cn.

**How to cite this article:** Guo Jian, He Yong, Xiao Qiangqiang, et al. Structure design of shaped charge for requirements of concrete crater diameter[J]. Trans. Nanjing U. Aero. Astro., 2015, 32(6):681-686.

<http://dx.doi.org/10.16356/j.1005-1120.2015.06.681>

$$D_c = \sqrt{\frac{A}{B}} \quad (1)$$

$$A = \frac{1}{(1 + \gamma)^2} v_j^2 D_0^2, \quad B = \frac{2R_t}{\rho_t}$$

where  $D_c$  is the penetration crater of jet,  $v_j$  the velocity of jet,  $D_0$  the diameter of jet,  $\gamma = \sqrt{\frac{\rho_t}{\rho_j}}$ , where  $\rho_t$  is the density of target,  $\rho_j$  the density of jet,  $R_t$  the penetration resistance of target.

Eq. (1) shows that the velocity and diameter of jet head should satisfy the following relations

$$v_T D_T = (1 + \gamma) \sqrt{\frac{2R_t}{\rho_t}} D_{Tc} \quad (2)$$

where  $v_T$  is the velocity of jet head,  $D_T$  the diameter of jet head, and  $D_{Tc}$  the crater diameter of concrete.

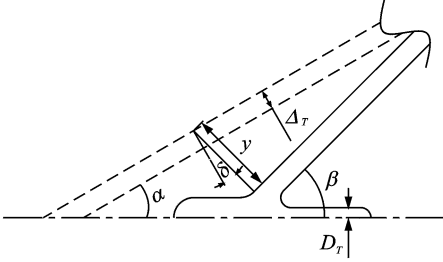


Fig. 1 Schematic of liner collapse

Fig. 1 deliberates the schematic of liner collapse. Since the distance between the elements at the top of the liner and charge axis is short, elements are quickly crushed to the axis driven by explosive detonation. Considering scattering angle  $\delta \approx 0^\circ$  and collapse angle  $\beta \approx \alpha$ , based on the formation theory of shaped charge jet, the velocity and the mass of jet head can be simplified as<sup>[12]</sup>

$$v_T = v_{T_0} \cot \frac{\alpha}{2} \quad (3(a))$$

$$m_T = m_{T_0} \sin^2 \frac{\alpha}{2} \quad (3(b))$$

where  $\alpha$  is the half cone angle of charge element,  $v_{T_0}$  the collapse velocity of elements at the top of the liner, and  $m_{T_0}$  the mass of elements at the top of the liner.

If  $y$  is the distance from element of the top liner to the axis and  $\Delta_T$  the wall thickness of element, the relationship between jet head diameter and wall thickness of the top liner can be obtained by geometry as

$$D_T = \sin \frac{\alpha}{2} \sqrt{\frac{\Delta_T}{\cos \alpha} \left( 2y + \frac{\Delta_T}{\cos \alpha} \right)} \quad (4)$$

Suppose that the move of element is only driven by explosive one-dimensional projection, and that the influence of lateral rarefaction waves and effect of elements can be ignored. Since the metal is not rigid body, surface pressure of projectile is actually not so high and detonation wave oblique impacts liner, collapse velocity of element at top liner is

$$v_{T_0} = \frac{1}{8} (\cos \varphi + 0.68) \frac{\rho_e l_T D}{\rho_j \Delta_T} \quad (5)$$

where  $\varphi$  is the angle from detonation wave front to tangent plane of liner element,  $l_T$  the length effective charge corresponding to liner element,  $\rho_e$  the density of the explosive, and  $D$  the detonation velocity.

To charge in top liner, we have

$$l_T = \frac{R_k - y}{2 \cos^2 \left( \frac{\alpha}{2} \right)} \quad (6)$$

where  $R_k$  is charge radius.

Substitute Eqs. (5, 6) into Eq. (3(a)), the velocity of jet head can be obtained. Then substitute Eqs. (3(a), 4) into Eq. (2), we obtain

$$\frac{1}{16} \frac{\rho_e (R_k - y)}{\rho_j \cos^2 \left( \frac{\alpha}{2} \right)} (\cos \varphi + 0.68) D \sqrt{\frac{1 + 2y \cos \alpha}{\Delta_T \cos^2 \alpha}} = (1 + \gamma) \sqrt{\frac{2R_t}{\rho_t}} D_{Tc} \quad (7)$$

When  $D_{Tc}$  is the crater diameter, the relationship of  $\Delta_T$ ,  $\alpha$ ,  $\varphi$  and  $y$  should satisfies Eq. (7). If any three of them are known, the fourth can be calculated. Therefore, by using the parameters of the top liner, structure can be designed, so as to obtain the required crater diameter on concrete.

## 1.2 Calculation verification

### 1.2.1 Cooper liner structure

The diameter of shaped charge is  $\varnothing 60$  mm and crater diameter on concrete is 0.6 times the charge diameter, that is  $D_{Tc} = 36$  mm. The explosive is JH-2, with  $\rho_e = 1.7$  g/cm<sup>3</sup>,  $D = 8.4$  mm/ $\mu$ s. The martial of liner is OFHC with  $\rho_j = 8.93$  g/cm<sup>3</sup>. Concrete is C35 with  $\rho_t = 2.4$  g/cm<sup>3</sup> and  $R_t = 68$  MPa<sup>[13]</sup>.

The charge structure is K type. Half cone

angle is  $\alpha = 60^\circ$ . The distance from element at the top liner to axis  $y$  is 1.6 mm. The diameter of waveform regulator is  $\varnothing 52$  mm and the angle of incidence of detonation wave is  $\varphi = 0^\circ$ .

We can get  $\Delta_T = 1.74$  mm by Eq (7). Through parameters of element at the top liner,  $v_T = 5.35$  mm/ $\mu$ s and  $D_T = 2.4$  mm can be obtained by Eq. (3(a)) and Eq. (4) respectively. To simplify the calculation during inverse design of the top structure of liner, we approximately set  $\delta \approx 0$ ,  $\beta \approx \alpha$ , so jet head velocity of the actual charge structure should be lower than the calculated value, and the head diameter is higher than calculation values.

According to the structure of liner top by inverse design,  $\varnothing 60$  mm shaped charge structure is shown in Fig. 2.

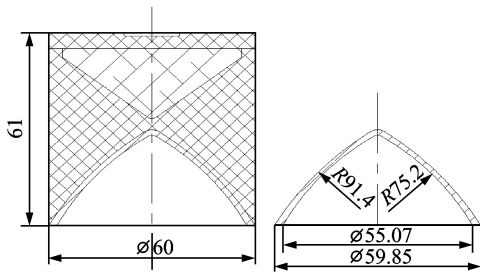


Fig. 2 Inversion structure of  $\varnothing 60$  mm shaped charge liner

### 1.2.2 Ti-alloy liner structure

The diameter of shaped charge is  $\varnothing 142$  mm and crater diameter on concrete is 0.7 times the charge diameter, that is  $D_{Tc} = 99$  mm. The explosive is Octol, with  $\rho_e = 1.78$  g/ $\text{cm}^3$  and  $D = 8.48$  mm/ $\mu$ s. The material of liner is Ti-alloy with  $\rho_l = 5.6$  g/ $\text{cm}^3$ . Concrete is C40 with  $\rho_t = 2.4$  g/ $\text{cm}^3$  and  $R_t = 80$  MPa<sup>[13]</sup>.

The charge structure is K type. The half cone angle is  $\alpha = 48^\circ$ . The distance from element at the top liner to axis  $y$  is 6 mm. The diameter of waveform regulator is  $\varnothing 132$  mm and the angle of incidence of detonation wave is  $\varphi = 0^\circ$ .

$\Delta_T = 6.48$  mm can be calculated by Eq. (7). With parameters of element at the top liner,  $v_T = 7.65$  mm/ $\mu$ s and  $D_T = 6$  mm can be obtained by Eq. (4(a)) and Eq. (6), respectively.

According to the structure of liner top by inverse design,  $\varnothing 142$  mm shaped charge structure is shown in Fig. 3.

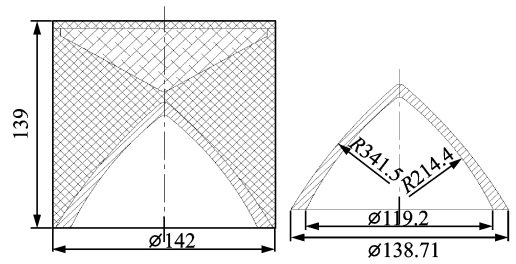


Fig. 3 Inversion structure of  $\varnothing 142$  mm shaped charge liner

## 2 Experiment and Analysis

### 2.1 X-ray experiment

X-ray experiment site layout for  $\varnothing 60$  mm shaped charge is shown in Fig. 4. Experiments were conducted four times, and the results are shown in Figs. 5—8.



Fig. 4 X-ray experiment site

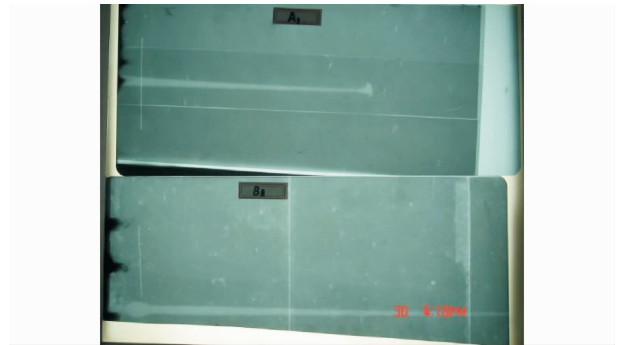


Fig. 5 X-ray of the first charge ( $50 \mu$ s,  $80 \mu$ s)

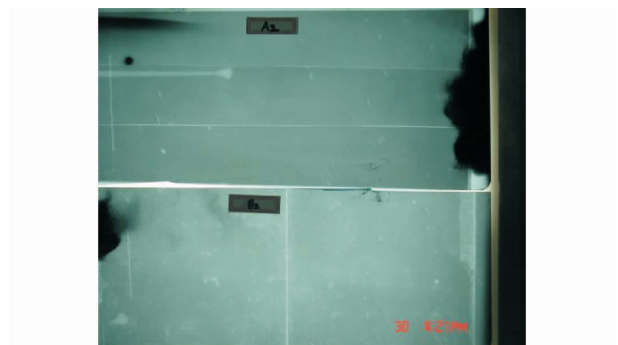


Fig. 6 X-ray of the second charge ( $40 \mu$ s,  $100 \mu$ s)

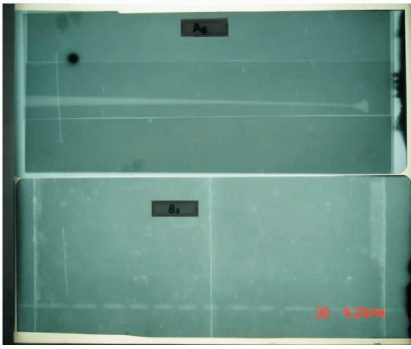


Fig. 7 X-ray of the third charge (60  $\mu$ s, 155  $\mu$ s)

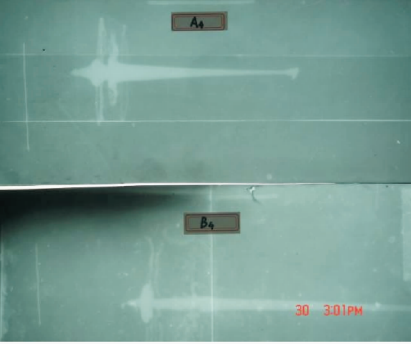


Fig. 8 X-ray of the fourth charge (30  $\mu$ s, 60  $\mu$ s)

Head velocity of shaped charge jet was about 5 000 m/s. Head diameter was about 3.5 mm. The tail velocity was about 1 265 m/s and the tail diameter was about 14.5 mm by measuring. X-ray showed that the calculation result was basically consistent with the basic X-ray experimental results. Compared with inverse design theoretical results, calculated value of head velocity was higher and head diameter was smaller which is in accordance with the results of the analysis because the theoretical analysis ignores flying angle and crushing angle changes of element at top liner.

## 2.2 Experiment on crater ability

### 2.2.1 Cooper liner

Standard C35 concrete target used in test has two kinds of thickness, 0.5 and 1 m. The stand-off is 100 mm (1.7 Cal.). Test site layout is shown in Fig. 9. Test was conducted three times. The first and the second target plate thicknesses were 500 mm. The third one was 1 000 mm, and the holes on the concrete are shown in Figs. 10—12.

The first in-crater diameter was 35 mm, and



Fig. 9 Test site layout of  $\varnothing$ 60 mm shaped charge penetrating concrete



Fig. 10 In-crater of the first  $\varnothing$ 60 mm shaped charge

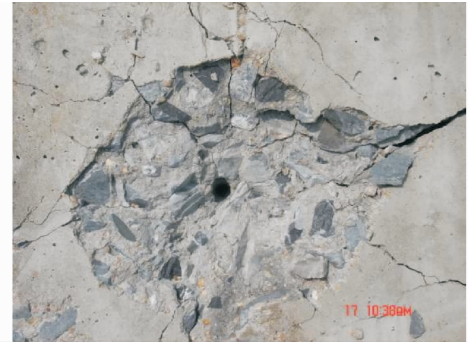


Fig. 11 In-crater of the second  $\varnothing$ 60 mm shaped charge



Fig. 12 In-crater of the third  $\varnothing$ 60 mm shaped charge

the out-crater diameter was 15 mm. The second in-crater diameter was 36 mm, and the out-crater diameter was 15 mm. The third target thickness was 1 000 mm. The penetration depth was 650 mm, and the in-crater diameter was 35 mm.

The test results are shown in Table 1.

**Table1 Test results of  $\varnothing 60$  mm shaped charge**

No.	Target thickness/mm	In-crater diameter/mm	Out-crater diameter/mm	Penetration depth/mm
1	500	35	15	Penetration
2	500	36	15	Penetration
3	1 000	35		650

When stand-off was 100 mm, the penetration depth of  $\varnothing 60$  mm shaped charge penetrating standard C35 concrete was 650 mm (about 10.8 Cal.) and in-crater diameter was 36 mm (0.6 Cal.), which agreed with the inverse design goal that  $\varnothing 60$  mm shaped charge penetrating diameter on concrete is larger than 0.6 Cal.

### 2.2.2 Ti-alloy liner

The thickness of standard C40 concrete target used in test was 1.2 m. The stand-off is 307 mm (2.2 Cal.). The in-crater hole on the concrete is shown in Fig. 13.



Fig. 13 In-crater of  $\varnothing 142$  mm shaped charge

The 1.2 m thick concrete target was penetrated. The in-crater diameter was 100 mm (0.7 Cal.), and the out-crater diameter was 70 mm (0.5 Cal.) which reached the inverse design goal that  $\varnothing 142$  mm shaped charge penetrating diameter on concrete is larger than 0.7 Cal.

## 3 Conclusions

We analyzed the velocity and the diameter of the jet head when shaped charge jet crater diameter met certain requirements by using the theories of shaped jet formation and crater diameter growth during jet penetrating concrete. The structure parameters of  $\varnothing 60$  mm and  $\varnothing 142$  mm

shaped charge were investigated with the required crater diameter. The structure of shaped charge was designed, and the head velocity and diameter were obtained by calculation.

By ignoring flying angle and crushing angle change, the calculated head velocity was higher than the actual value and the calculated head diameter was lower than the actual value, which was confirmed by X-ray experiments. The penetration power experiment indicated that when stand-off was 100 mm, the penetration depth of  $\varnothing 60$  mm shaped charge penetrating standard C35 concrete was 650 mm (about 10.8 Cal.) and in-crater diameter was 36 mm (0.6 Cal.), and  $\varnothing 142$  mm shaped charge penetrated 1.2 m standard C40 concrete and in-crater diameter was 100 mm (0.7 Cal.). The experiment validated our design.

## References:

- [1] Wang Shuyou. Penetration mechanism of reinforced concrete targets by tandem warhead [D]. Nanjing: Nanjing University of Science and Technology, 2006. (in Chinese)
- [2] Liu He, Wang Feng, Wang Yucai, et al. Oil well perforation technology: Status and prospects [J]. Petroleum Exploration and Development, 2014, 41(6): 731-737. (in Chinese)
- [3] Huerta M, Vigil M G. Design, analyses, and field test of a 0.7 m conical shaped charge [J]. International Journal of Impact Engineering, 2006, 32(8): 1201-1213.
- [4] Xiao Q Q, Huang Z X, Zu X D, et al. Penetration research of jacketed jet into concrete [J]. International Journal of Impact Engineering, 2013, 54: 246-253.
- [5] Zhou Quan. Multi-objective optimization design of penetration depth and crater diameter of shaped charge [D]. Nanjing: Nanjing University of Science and Technology, 2007. (in Chinese)
- [6] Ma Jianfu. Study on the mechanism of penetrating into concrete using shaped charge structures [D]. Taiyuan: North University of China, 2007. (in Chinese)
- [7] Szendrei T. Analytical model of crater formation by jet impact and its application to calculation of pene-

- tration curves and hold profiles[C]//7th Nternational Symposium of Ballistics. Hague, Netherlands: [ s. n. ],1983: 575-583.
- [8] Szendrei T. Link between axial penetration and radial crater expansion in hypervelocity impact[C]// 17th International Symposium of Ballistics. Midrand, South Africa: International Ballistics Committee, 1998: 25-32.
- [9] Held M. Verification of the equation for radial crater growth by shaped charge jet penetration[J]. International Journal of Impact Engineering, 1995, 17(1/2/3): 387-398.
- [10] Held M, Huang N S, Jiang D, et al. Determination of the crater radius as a function of time of a shaped charge jet that penetrates water[J]. Propellants, Explosives, Pyrotechnics, 1996, 21(2): 64-69.
- [11] Held M, Kozhushko A A. Radial crater growing process in different materials with shaped charge jets [J]. Propellants, Explosives, Pyrotechnics, 1999, 24(6): 339-342.
- [12] Wang Ruce, Zhao Guozhi. Projectile terminal effects [M]. Version 1. Beijing: Beijing University of Science and Technology Press, 1993. (in Chinese)
- [13] Xiao Q Q, Huang Z X, Zhu C S, et al. Calculation of depth and crater diameter for the supersonic penetration of shaped charge jet into concrete[J]. Propellants, Explosives, Pyrotechnics, 2013, 38(2): 224-231.

(Executive Editor: Zhang Bei)

