

Occupant Restraint System Simulation and Optimization Based on TESW

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Abstract: Integrated into the development process of a chinese independent brand class sedan, optimization about occupant restraint system associated with dummy chest deceleration is studied. Based on this simulated vehicle deceleration and the target vehicle's chest deceleration, tipped equivalent square wave (TESW) is calculated by combining the average stiffness k of occupant restraint system and the average free flight time t^* from the existant C-NCAP (China new car assessment program) tested cars. After proposing modeling regulations of occupant restraint system and establishing mathematical dynamic modelling (MADYMO) for occupant restraint system of the target vehicle, four optimization design parameters namely vent area A , load limit L , seat belt extension ratio B and pre-tension force F are selected by weighted injury criteria (WIC) rule and the first-order response surface method. The four parameters have been optimized by using orthogonal test design of four factors with five levels and the optimum combination $A_5L_1B_1F_5$ has been chosen by range and variance analyses. The results show that occupant restraint system performance has been optimized and improved, while meeting the chest deceleration calculation peak based on TESW.

Key words: full frontal impact; tipped equivalent square wave; occupant restraint system

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0 Introduction

In the process of full frontal impact, some scholars, engineers and technicians' researches revealed that chest deceleration not only connected with the body structure, but also it was affected by occupant restraint system^[1-3]. In particular, the peak of dummy chest deceleration had a certain relationship among the occupant restraint system, the initial impact velocity, the body structure and occupant response^[4-7]. Thus Huang^[8] assumed and proved that in the process of 100% frontal impact, dummy chest deceleration \ddot{x}_o and body deceleration \ddot{x}_v existed following relationship: $\ddot{x}_o = A \sin(\omega t' + \varphi) + \ddot{x}_v$. According to the data of the similar structure of China new car assessment program (C-NCAP) tested star

cars, Tian Sheng et al.^[9] proposed to design target vehicle by equivalent dual trapezoids wave (EDTW) envelope curves and the average free flight time t^* and the average occupant restraint system stiffness k , designing body structure based on EDTW and designing occupant restraint system based on tipped equivalent square wave (TESW) by using a fitting combination scheme. At the same time, Tian Sheng et al.^[9] calculated chest deceleration based on equivalent square wave (ESW), TESW and EDTW comparably and found that chest deceleration peak based on TESW is most close to the actual one. On this basis, the occupant restraint system based on TESW will be optimally designed by simulation in the paper.

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1 Calculation of Dummy Chest Deceleration

The better program curve of body deceleration is gained by simulation shown as Fig. 1, which is lined with the principle of high in the front and low in the behind. According to Fig. 1, when the deceleration is zero again, the moment is $t_7 = 76.50$ ms.

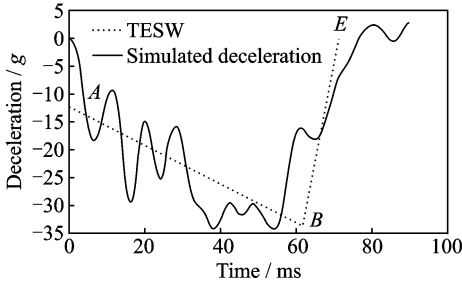


Fig. 1 Vehicle simulation deceleration \ddot{x}_v and TESW

The speed curve and displacement curve can be integrated from the vehicle deceleration curve respectively. we can see from the speed curve that when the speed is zero, the moment t_m is 61.69 ms, and when the moment t_7 is 76.50 ms, the speed v_{t_7} is $-1\,580.63$ mm/s. We can also judge the maximum displacement $C = 494.79$ mm from the displacement curve, and calculate the waveform of TESW based on body deceleration in Fig. 1.

When $v_0 = 50$ km/h and $C = 494.79$ mm, the centroid time t_c is calculated as

$$t_c = \frac{C}{v_0} = \frac{494.79 \times 3\,600}{50 \times 10^6} = 35.62(\text{ms}) \quad (1)$$

since $\frac{t_c}{t_m} = \frac{35.62}{61.69} \approx 0.577 > 0.5$ and meet the

requirement of $\frac{1}{3} \leq \frac{t_c}{t_m} \leq \frac{2}{3}$, the fitting TESW is rear-loaded pulse.

Substituting $v_0 = 50$ km/h, $t_c = 35.62$ ms and $t_m = 61.69$ ms into the Eqs. (2), (3), respectively, calculating

$$\ddot{x}_v(0) = \frac{2v_0}{t_m^2}(3t_c - 2t_m) = -12.29g \quad (2)$$

$$\ddot{x}_v(t_m) = \frac{2v_0}{t_m^2}(t_m - 3t_c) = -33.61g \quad (3)$$

Substituting $t_m = 61.69$ ms, $\ddot{x}_v(0) = -12.29g$ and $\ddot{x}_v(t_m) = -33.61g$ into Eq. (4), getting the slope of the line $AB(s_1)$

$$s_1 = \frac{\ddot{x}_v(t_m) - \ddot{x}_v(0)}{t_m} = -0.345\,6g\,\text{ms}^{-1} \quad (4)$$

The equation of AB line in Fig. 2 is: $\ddot{x}_v = -0.345\,6t - 12.29$ ($0 \leq t \leq 61.69$ ms). If the average free flight time t^* is 16.01 ms in C-NCAP frontal crash test, the equation can also be expressed as $\ddot{x}_v = -0.345\,6t' - 17.82$ ($0 \leq t' \leq 45.68$ ms), and $\ddot{x}_v(t^*) = -17.82g$.

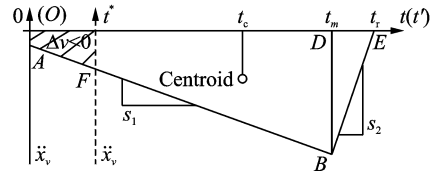


Fig. 2 TESW

Because v_{t_7} is $-1\,580.63$ mm/s, the velocity difference of rebound phase Δv_r is $-1\,580.63$ mm/s. Calculating the end time t_r of body rebound based on TESW

$$t_r - t_m = \frac{2\Delta v_r}{\ddot{x}_v(t_m)} \quad (5)$$

$$t_r = 61.69 + \frac{2 \times (-1\,580.63)}{-33.61 \times 9\,810} \times 10^3 \approx 71.28(\text{ms}) \quad (6)$$

Substituting $t_m = 61.69$ ms, $t_r = 71.28$ ms and $\ddot{x}_v(t_m) = -33.61g$ into Eq. (7), getting the slope of the line $BE(s_2)$

$$s_2 = \frac{0 - \ddot{x}_v(t_m)}{t_r - t_m} = 3.504\,69g\,\text{ms}^{-1} \quad (7)$$

The equation of BE line in Fig. 2 is: $\ddot{x}_v = 3.504\,69t - 249.81$ (61.69 ms $\leq t \leq 71.28$ ms) or $\ddot{x}_v = 3.504\,69t' - 193.70$ (45.68 ms $\leq t' \leq 55.27$ ms).

Therefore, the three key points of TESW waveform based on the simulated body deceleration are: $A(0, -12.29g)$, $(61.69$ ms, $-33.61g)$ and $E(71.28$ ms, $0)$. The fitting TESW waveform is shown as Fig. 2.

If $k = 0.122\,6g\,\text{mm}^{-1}$ (the average stiffness of existing similar structures star vehicle's occupant restraint system), $\omega = \sqrt{0.122\,6} \approx$

$$34.68 \text{ s}^{-1} = 0.03468 \text{ ms}^{-1}.$$

Calculating the shaded area Δv referring to Fig. 2 shown as Eq. (8). In accordance with Eqs. (9), (10), respectively, calculating the amplitude A and phase angle φ , then in accordance with Eq. (11) designing and calculating the dummy chest deceleration of target car.

$$\Delta v = \frac{1}{2} [\ddot{x}_v(0) + \ddot{x}_v(t^*)] \cdot t^* \approx -2.36 \text{ m/s} \quad (8)$$

$$A = -\sqrt{(\omega \cdot \Delta v)^2 + [\ddot{x}_v(t^*)]^2} = -19.68g \quad (9)$$

$$\varphi = -\arctan \frac{\ddot{x}_v(t^*)}{\Delta v \cdot \omega} = -1.132 \quad (10)$$

$$\ddot{x}_o = A \sin(\omega t' + \varphi) + \ddot{x}_v \quad (11)$$

Getting TESW through the simulated body deceleration curve, then chest deceleration is expressed as Eq. (12) based on TESW and shown as Fig. 3.

$$\ddot{x}_o = -19.68 \sin(0.03468t' - 1.132) + \begin{cases} -0.3456t' - 17.82 & 0 \leq t' \leq 45.68 \text{ ms} \\ 3.50469t' - 193.70 & 45.68 \text{ ms} \leq t' \leq 55.27 \text{ ms} \end{cases} \quad (12)$$

$$\ddot{x}_{o\max} = -19.68 \sin(0.03468 \times 45.68 - 1.132) - 33.61 = -42.20g \quad (13)$$

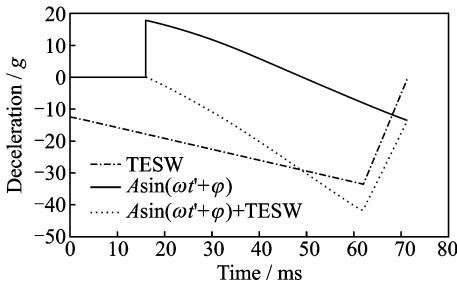


Fig. 3 Dummy chest deceleration based on TESW from simulation

Thus, after calculating the average free flight time $t^* = 16.01 \text{ ms}$ and the stiffness of occupant restraint system $k = 0.1226 \text{ g} \cdot \text{mm}^{-1}$ through the star car of similar structure, the dummy chest deceleration of the target car has been calculated based on the simulated body deceleration.

2 Modeling of Occupant Restraint System

2.1 Modeling of interior

The accurate mathematical dynamic modeling (MADYMO) occupant restraint system of interior and components depends on the actual size and installation relationship, which can be selected from the general arrangement or design drawings. Because the installation of design products from different manufacture may be different, there will be some points in the modeling which need to pay strong attention to. The established multi-body (MB) model of the interior parts is shown as Fig. 4.

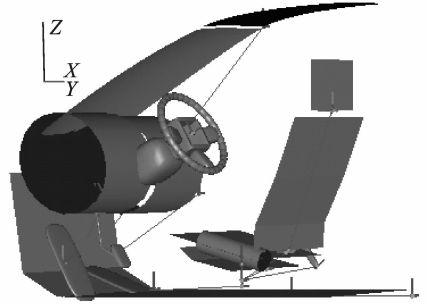


Fig. 4 MB model of interior parts

2.2 Modeling of seat belt

The modeling and positioning of seat belt have an important impact on accuracy of the simulation results. Retractor, guide groove, height adjuster, D ring, buckle, anchor and other positional parameters determine the ribbon trend and connection of the seat belt model. Ribbon can be modeled by MB or the mix of MB and finite element (FE). The sliding of the seat belt in the dummy body surface can be simulated by MB and FE method, and the penetration effect of the seat belt fabric, which is embedded in the dummy body surface, can be simulated by orthotropic friction coefficient. The seat belt is modeled by MB and FE methods in this paper as shown in Figs. 5, 6.

2.3 Modeling of airbag

The FE airbag model includes the reference model and the initial model in MADYMO. Refer-

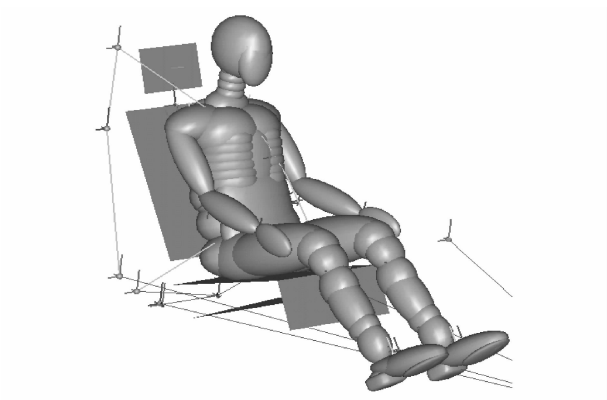


Fig. 5 MB modeling of belt

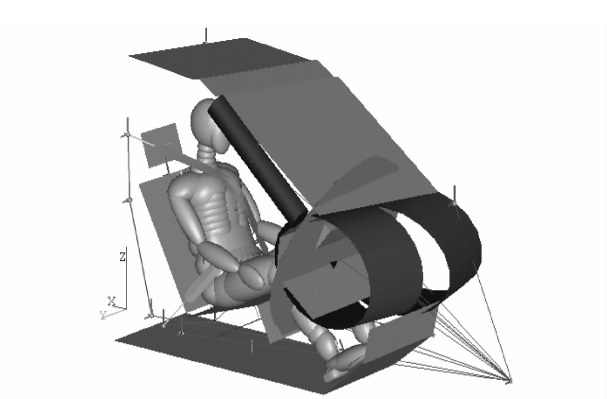


Fig. 6 FE modeling of belt

ence model made by pre-treatment meshing software (e. g. Hypermesh) is the real shape of the airbag's geometry without initial stress shown as Fig. 7; Initial model is the airbag which has been folded shown as Fig. 8, whose size and shape are the same as the ones of the real vehicle' air-bag. In MADYMO, it will automatically search airbag's reference model when initial model is inflated.

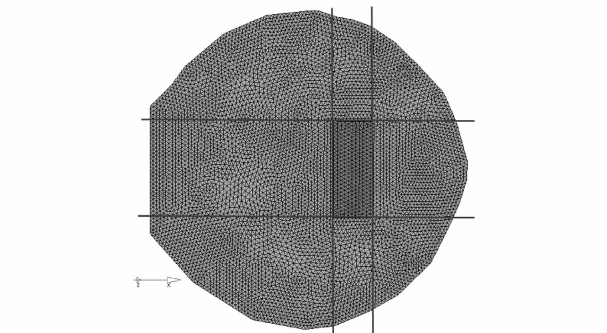


Fig. 7 Airbag reference model

The fabric and hole materials of airbag need be set. While airbag chamber being set, we need

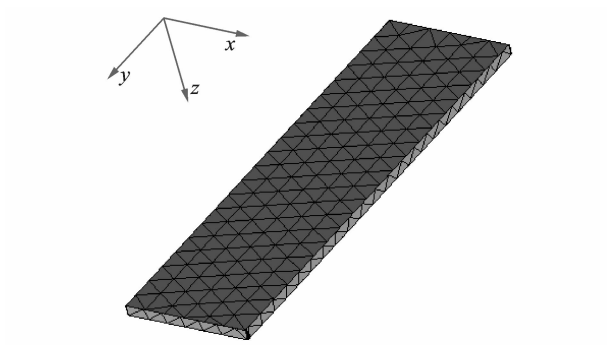


Fig. 8 Airbag initial model

to understand the parameters of the gas generator, such as ignition time (Switch), the gas mass flow (Mass-flow-rate) and gas ingredient (Gas).

2.4 Dummy positioning

Accurate dummy positioning is very important to the simulation results in MADYMO. Commonly there are two dummy positioning methods;directly input the measured location parameter values of the physical dummy before test (See Fig. 9), or just exert the gravitational field to a dummy in the pre-simulation to make dummy and seat reach the static equilibrium state under the interaction of the parts (See Fig. 10). In fact two methods are used in combination in the pa-per.

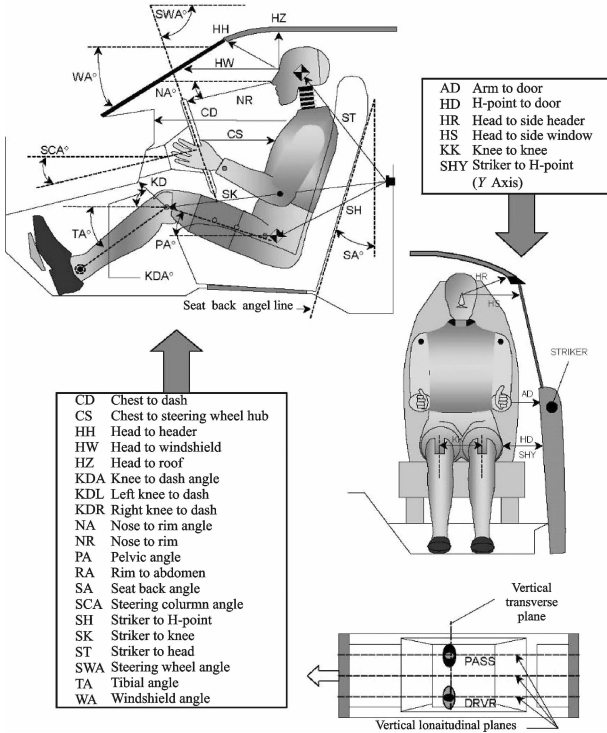


Fig. 9 Dummy Position 1 (Position data)

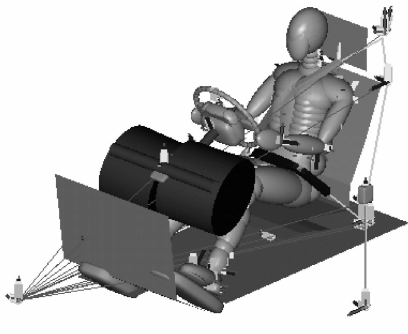


Fig. 10 Dummy Position 2

3 Simulation and Optimization of Occupant Restraint System

The evaluation of occupant restraint system design depends on test scores of dummy. Weighted factors were introduced by Viano and Arepally^[10] from general motors (GM) in 1990 to evaluate the extent of dummy injury by integrating injury indexes together with weighted method and to fully evaluate the performance of occupant restraint system by using weighted injury criterion (WIC). Comprehensive evaluation index WIC is calculated by using head impact criteria (HIC), chest accelerations and compressions, and thigh's forces. Weighted coefficient of each index in Eq.(14) shows that the injury extent which comes from the statistical analyses on a large number of accidents. The lower the WIC value is, the better the protect performance of occupant restraint system is.

$$\begin{aligned} \text{WIC} = & 0.6 \left(\frac{\text{HIC}}{1\,000} \right) + 0.35 \left(\frac{C_{3\text{ ms}}}{60} + \frac{C_{\text{comp}}}{76.2} \right) / 2 + \\ & 0.05 \left(\frac{F_{\text{FL}} + F_{\text{FR}}}{20.0} \right) \end{aligned} \tag{14}$$

where HIC denotes comprehensive performance indexes of the head; $C_{3\text{ ms}}$ the chest deceleration value during 3 ms; C_{comp} (mm) the chest compression; F_{FL} (kN) the maximum axial force of the left thigh; and F_{FR} (kN) the maximum axial force of the right thigh.

The first-order linear response surface model of WIC has been built by orthogonal experiment method to select four optimization design parame-

ters, namely vent area A , load limit L , seat belt extension ratio B and pretension force F for occupant restraint system.

After selecting four parameters as the design variables of occupant restraint system, considering four changes of the initial value in the upper and lower symmetry which lead to five levels shown as Table 1. Therefore, this is a four factors and five levels orthogonal experimental design, selecting the orthogonal table $L_{25}(5^4)$.

Table 1 Four factors and five levels

Level	A/mm^2	L/kN	$B/\%$	F/kN
1	1 005.28	2.05	6	1.50
2	1 130.94	2.30	10	1.65
3	1 256.60	2.55	13	1.80
4	1 382.26	2.80	17	1.95
5	1 507.92	3.05	20	2.10

It should be noted that dummy chest deceleration peak \ddot{x}_{omax} in x -direction introduced has been considered for the total occupant restraint system, including the steering wheel, so outputting the dummy HIC of the driver's side, chest synthetic acceleration $C_{3\text{ ms}}$, chest compression C_{comp} , the left thigh axial pressure F_{FL} , and the right thigh axial pressure F_{FR} in accordance with orthogonal experiment design of the four factors and five levels, then calculating WIC according to Eq.(14). In order to observe the peak deceleration \ddot{x}_{omax} of dummy chest in x -direction whether meets $-42.2g$ which is computed in the first part or not, in particular, the dummy chest peak deceleration \ddot{x}_{omax} in x -direction has been calculated. Increasing one program of initial value on the basis of the 25 trials, the obtained results are shown as No.0 test of Table 2 when the four design parameters being taken the initial value.

If only take the minimum WIC (0.457 54) and absolute the minimum \ddot{x}_{omax} ($-41.489g$) as the standard, we select No.22 test combination in Table 2 ($A_5L_2B_1F_5$). However, the chest deceleration peak \ddot{x}_{omax} has been calculated (Equal to $-42.2g$) based on TESW in the first part of this

paper. Therefore, we choose the chest deceleration peak \ddot{x}_{omax} close to $-42.2g$ to verify ideas of this paper. But taking a combination of direct observation to the test results cannot completely guarantee the optimal combination, since we just make a part of the test. Therefore, we need to do the range and variance analyses, and make a comparative choice.

The optimal candidate solution is $A_4L_4B_2F_5$ by variance analysis and the optimal candidate solution is $A_5L_1B_1F_5$ by range analysis. Three optimal candidate solutions include $A_4L_4B_2F_5$ (No. 19 test), $A_5L_2B_1F_5$ (No. 22 test), and $A_5L_1B_1F_5$, but $A_5L_1B_1F_5$ combination does not appear in orthogonal test which need to remodel and simulate

in MADYMO. The results of simulation are shown as Table 2, comparing with No. 0, No. 19 and No. 22 test.

Comparing the schemes in Table 2, in addition to decline of the major damage index value, such as WIC and HIC, \ddot{x}_{omax} should be close to the calculated peak ($-42.2g$), too. Not only WIC and HIC of $A_5L_1B_1F_5$ have been decreased, but also $-42.283g$ is the closest to $-42.2g$ (\ddot{x}_{omax}). Although the left and right thigh axial forces of $A_5L_1B_1F_5$ have been increased, the scores are still full scores (Full scores are 2 points). Therefore, we choose $A_5L_1B_1F_5$ as the final optimal program of occupant restraint systems (Shown as bold in Table 2).

Table 2 Choosing scheme

No.	HIC	$C_3\text{ ms}/g$	\ddot{x}_{omax}/g	$C_{\text{comp}}/\text{mm}$	F_{FL}/kN	F_{FR}/kN	WIC
0	505.98	43.083	-43.179	29.566	1.280	0.940	0.502 70
19	467.61	41.914	-42.431	30.029	1.278	0.967	0.477 39
Percentage	-7.58%	-2.71%	-1.73%	1.57%	-0.16%	2.87%	-5.03%
22	443.75	41.4	-41.489	28.216	1.304	0.994	0.457 54
Percentage	-12.30%	-3.91%	-3.91%	-4.57%	1.88%	5.74%	-8.98%
$A_5L_1B_1F_5$	445.77	41.41	-42.283	28.393	1.288	0.976	0.459 10
Percentage	-11.90%	-3.88%	-2.08%	-3.97%	0.62%	3.83%	-8.67%

4 Conclusions

(1) First, after the simulated and optimized body deceleration has been calculated to TESW, the dummy chest deceleration peak \ddot{x}_{omax} in x -direction is equal to $-42.2g$ based on TESW by a set of complete fitting combination design methodology of car full frontal impact safety.

(2) \ddot{x}_{omax} and WIC known as the objective functions identify the quantity to be minimized in order to optimize the occupant restraint system.

(3) The occupant restraint system is modeled by using MADYMO and modeling approach of the target vehicle is described, including interior, seat belt, airbag as well as the positioning of dummy.

(4) The four design parameters (vent area

A , load limit L , seat belt extension ratio B and pretension force F) have been optimized by using four factors and five levels orthogonal experimental design.

(5) The calculation results show that the dummy injury WIC has been decreased by 8.67% and restraint system performance has been optimized and improved in the process of full frontal impact.

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