# Removing Random-Valued Impulse Noises by a Two-Staged Nonlinear Filtering Method

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Abstract: Digital images are frequently contaminated by impulse noise (IN) during acquisition and transmission. The removal of this noise from images is essential for their further processing. In this paper, a two-staged nonlinear filtering algorithm is proposed for removing random-valued impulse noise (RVIN) from digital images. Noisy pixels are identified and corrected in two cascaded stages. The statistics of two subsets of nearest neighbors are employed as the criterion for detecting noisy pixels in the first stage, while directional differences are adopted as the detector criterion in the second stage. The respective adaptive median values are taken as the replacement values for noisy pixels in each stage. The performance of the proposed method was compared with that of several existing methods. The experimental results show that the performance of the suggested algorithm is superior to those of the compared methods in terms of noise removal, edge preservation, and processing time.

**Key words:** image de-noising; random-valued impulse noise; nonlinear filter; noisy pixel detection; two-stage detection and correction method; cascaded stages; directional differences

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#### 0 Introduction

In image processing, noise reduction is a necessary and challenging step, which further influences the performance of subsequent analyses. Image noises are of various types, such as amplifier noise, film grain, shot noise, speckle noise, and impulse noise. During acquisition and transmission, digital images are commonly corrupted by impulse noise (IN). There are two types of INs: fixed-valued impulse noise (FVIN) and random-valued impulse noise (RVIN)<sup>[1]</sup>. In this study, we focused on removing RVIN while preserving the details and edges of the image. Let I(i, j) and I'(i, j) be the intensity values at pixel location (i, j) of the original and noisy image, respectively, n(i, j) the noise value at location

(i, j), and  $[I_{\min}, I_{\max}]$  the dynamic range of the intensities of the original image. Then, the IN model with noise probability p using the Bernoulli uniform noise model can be given as [2]

$$I'(i,j) = \begin{cases} I(i,j) & \text{With probability } p \\ n(i,j) & \text{With probability } 1-p \end{cases}.$$

For FVIN, a noisy pixel can take the value of either  $I_{\min}$  or  $I_{\max}^{[3-4]}$ , whereas for RVIN it can be any random value between  $I_{\min}$  and  $I_{\max}^{[5-6]}$ .

Non-linear filtering techniques, of which median filters are an example, are used frequently to remove IN. The efficiency of the standard median filter (SMF)<sup>[1]</sup> is good but it blurs the details and edges when the noise density exceeds  $50\%^{[7-8]}$ . Several variants of SMF, such as the adaptive median filter (AMF)<sup>[3]</sup> and center-weighted median filter (CWMF)<sup>[9]</sup>, were designed to over-

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come this problem. These methods process all the corrupt, as well as the uncorrupt pixels, which results in blurring, distortion, or elimination of the structural details.

To achieve ideal filtering, the filter should treat only the noisy pixels without affecting the noise-free pixels and therefore a noise detection procedure must be adopted before the filtering process is performed<sup>[10]</sup>. Some noise removal methods using noise detectors were proposed. For example, the tri-state median filter (TSMF)[11] integrates SMF and CWMF in a noise detection framework, the recursive adaptive center-weighted median filter (ACWMF)[12] realizes the impulse detection based on the differences between the current pixel and the outputs of a CWM filter with varying weights, and the switching median filter (SwMF)<sup>[13]</sup> detects noisy pixels using the results of four convolutions obtained from one-dimensional Laplacian operators. Besides this, wavelet transform and the contourlet based edge preserving methods were also proposed. Weng et al. [14] used translation-invariant (TI) dyadic wavelet transform to suppress the noise and Wu et al. [15] applied contourlet modulus maxima technique to high frequency image portion for edge detection during noise elimination. The disadvantages of the aforementioned decision and transformation based filters are that predefined thresholds are required and possible edge pixels in corresponding regions are not specially considered during replacement, and thus, the edge and structural details remain unrecovered. Recently, Shan and Zhu<sup>[16]</sup> presented a local similarity pattern-based method. In this method, corrupt pixels are restored using the normalized weighted sum of the good pixels in their neighborhoods. However, the selection of separate weights for a smooth and an edge region renders the filtering process complex. In the method presented in Ref. [17], a low-rank matrix approximation is used to preserve the texture detail in IN corrupted images and a weighted matrix is incorporated to estimate the distribution of spatial noises. This method is designed to detect and remove non-pointwise random-valued IN, i. e., very small noise blobs, efficiently. In the last few years, fuzzy logic-based filtering techniques have been used as a substitution for the previous noise detection and reduction methods<sup>[18-21]</sup>. For example, a hybrid filtering technique<sup>[22]</sup> detects noisy pixels using the asymmetric trimmed median filter (ATMF) and restores them by using ATMF combined with a fuzzy inference system. Fuzzy filters apply human decision-making strategies to classify noisy and noise-free pixels, but at the cost of an appropriate balance between noise elimination and edge protection.

To protect the edges, Awad<sup>[23]</sup> proposed a method that finds an optimal direction to be used as a scale to judge noisy pixels. Since the direction that has the most similar pixels is considered the optimal direction, the recovery of edges having pixels between which there is a greater difference is affected. Ebenezer et al. [24] proposed a decision-based algorithm that replaces detected noisy pixels with either the median intensity value or the intensity value of a certain nearby neighbor. This method resolves the blurring effect problem, but the three sorting steps of which it is comprised lead to a decrease in filtering efficiency. Vijayaragavan et al. [25] also contributed to blurred edge restoration and proposed a twostaged algorithm that calculates directional differences in four directions. The noisy pixel is replaced with the median value of the pixels corresponding to the directions having the least differences. This method is time-efficient, but noisy pixels that are very similar to their noise-free neighbors remain undetected and thus the filtering performance is affected. Lien et al. [26] proposed a method that uses a decision-tree-based noise detector and a complex edge preserving reconstruction design. Turkmen[27] proposed a fourphase method for the reinstatement of edges. In each phase, the noisy pixel is determined by respective statistical measures and replaced by the median value of its noise-free neighbors. This method is effective in terms of noise removal and edge restoration, but increases the processing time because the image must be scanned four times.

Here we propose a two-staged filtering method that addresses the problems of edge blurring and increases processing time encountered during RVIN removal. The proposed method is an improved and hybrid version of the techniques proposed by Vijayaragavan<sup>[25]</sup> and Turkmen<sup>[27]</sup>. In our method, the detection and correction of noisy pixels at each of the two stages are accomplished differently. The performance of the proposed method is compared with that of other median-based and some recently developed methods. Our method is found to yield a significantly better performance than other baseline methods in terms of noise removal, edge preservation, and processing time.

# 1 Proposed Method

The proposed algorithm comprises two cascaded noise detectors instead of four independent detectors as applied in Turkmen's method<sup>[27]</sup>. The replacement of noisy pixels is accomplished in a different manner in each stage in contrast to Turkmen's method<sup>[27]</sup>, where the same replacement mechanism is used in all phases. In stage I, a noisy pixel is detected by examining the mean values of the absolute differences between the test pixel and two subsets of its neighbors. If the results show that the test pixel is noisy, its value is replaced by the median value of its neighboring pixels; if the pixel is found to be noisefree, its noise-free character is verified again in the second stage. In stage II, the detection of a noisy pixel is achieved by comparing it with its neighborhood pixels in four directions. The test pixel is considered noisy when substantial differences exist between it and the pixels along more than two directions, and the median of the pixels from these directions is then used to replace the noisy pixel. Therefore, directional differences are used in noise detection instead of in the calculation of the replacement value as in Vijayaragavan' s method<sup>[25]</sup>. The unique aspects of our method are that noise detection is based on two different

criterions implemented in two stages respectively, a noise-free pixel is tested twice in one scan, and two different replacement values are used. Through this two-staged method, we detect and correct the noisy pixels in two cases. The objective of the first stage is to find the noisy pixels that are significantly different from their neighbors. The second stage uses directional differences not only to capture small-difference cases missed in stage I, but also to differentiate edge from noisy pixels, because the directional difference technique distinguishes the directions having obvious differences from those having unobvious ones. A complete description of the proposed algorithm is given in Section 1.1.

#### 1.1 Algorithm description

Consider a gray-scale noisy image I corrupted with RVIN and a sliding square test window  $W_{\rm T}$  of size  $3\times 3$  centered at test pixel I(i,j), given as

$$W_{\mathrm{T}} = \{ I(i+l, j+m) \mid -1 \leqslant l, m \leqslant 1 \}$$
 (1)

The noisy image is scanned by the test window and the proposed two-staged detection and correction method is applied. Let  $N_x$  be the set of all neighboring pixels in  $W_T$  written in an ascending order,  $\operatorname{Med}(N_x)$  be the median of all neighboring elements, and  $D_x$  be a distance vector set defined as  $D_x = \{ |I(i,j) - N_x)| | x = 1, \dots, 8 \}$ . Two statistical variables  $S_1$  and  $S_2$  based on  $D_x$  are defined as the mean value of the first three and the next two smallest  $D_x$  values, respectively. Assume that all elements in  $D_x$  are listed in an ascending order.  $S_1$  and  $S_2$  are calculated as

$$S_1 = 1/3 \sum_{x=1}^{3} D_x \tag{2}$$

$$S_3 = 1/2 \sum_{x=4}^{5} D_x \tag{3}$$

The first stage of the noise detection process starts

$$I(i,j) = \begin{cases} \text{noisy} & \text{If } S_1 > T_1 \text{ and } S_2 > T_2 \\ \text{noisefree} & \text{Otherwise} \end{cases}$$
 (4)

where  $T_1$  and  $T_2$  are the thresholds. If the value of Eq. (4) indicates that the test pixel is noisy, it is replaced by the median value of the last seven neighboring pixels. The first most similar neigh-

bor is excluded from the calculation of the replacement value because of its probability of being noisy. The test pixel, if detected as noise-free, will be tested again in stage  $\mathbb{I}$  for further assurance. In stage  $\mathbb{I}$ , four variables denoted by  $\Delta_{\rm S}$  are defined as the absolute differences between the intensity value of the test pixel and the mean intensity values of its neighboring pixels along four major directions, i. e., horizontal, vertical, left diagonal, and right diagonal. These four variables are calculated as

$$\begin{split} \Delta_{\rm H} = & \mid (I(i,j-1) + I(i,j+1))/2 - I(i,j) \mid \\ \Delta_{\rm V} = & \mid (I(i-1,j) + I(i+1,j))/2 - I(i,j) \mid \\ \Delta_{\rm L} = & \mid (I(i-1,j-1) + I(i+1,j+1))/2 - \\ & \quad I(i,j) \mid \\ \Delta_{\rm R} = & \mid (I(i-1,j+1) + I(i+1,j-1))/2 - \\ & \quad I(i,j) \mid \end{split}$$
 (5)

From the absolute differences given in Eq. (5), a variable cnt is defined as equals the number of  $\Delta_{\rm S}$  that is greater than  $T_{\rm 3}$ , and the pixel detected as cnt noise-free in stage I is tested again

$$I(i,j) = \begin{cases} \text{noisy} & \text{If } cnt > 2\\ \text{noise free} & \text{Otherwise} \end{cases}$$
 (6)

A detected noisy pixel is replaced by the median value of pixels in the directions having  $\Delta_{\rm S}$  greater than  $T_3$ . The rationale behind this replacement mechanism is that other elements of the discarded directions are very near to the test pixel and therefore they could also be noisy, while the pixels corresponding to the directions under *cnt* are noise-free. Therefore, the noisy pixel is replaced by the median value of noise-free pixels. The two-staged detection and correction method is now completed and the test window is moved to process the next pixel. The entire structure of the algorithm is depicted by the flow-chart given in Fig. 1.

#### 1.2 Logic of algorithm and threshold

The logic behind using two variables in the first stage is as follows.  $S_1$  helps distinguish a noisy pixel from its neighbors because the neighboring pixels of a noise-free test pixel in general possess similar characteristics. However, in the

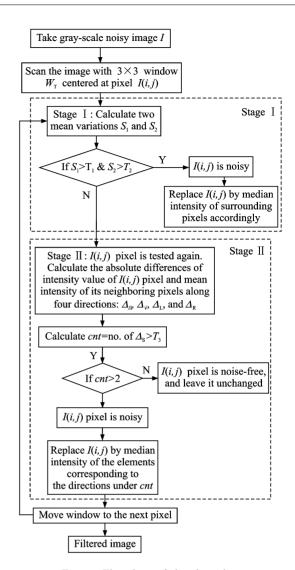


Fig. 1 Flowchart of the algorithm

case of an image corrupted with a high noise density, the nearest three neighbors of the test pixel may also be noisy and their intensity values may be very near those of the test pixel. In this case, the mean value obtained from Eq. (2) is very small and therefore some noisy pixels remain undetected. In order to avoid corrupt pixels escaping detection, the mean of the absolute differences between the intensity values of the central pixel and the next two most similar pixels is calculated, as given in Eq. (3). The test pixel is classified as noisy if the value of Eq. (3) is larger than some threshold. In addition, if the test pixel is an edge pixel there must be at least one more pixel, having almost the same intensity, and therefore, the number of similar neighbors may exceed three. Therefore, variable  $S_2$  is included to distinguish edge and noisy pixels. On the basis of the scenario stated above, the threshold values for  $T_1$  and  $T_2$  are kept smaller and greater, respectively. For  $T_3$ , a significantly larger threshold value is selected, because in the practical scenario of stage  $\mathbb{I}$  not only are the corrupt pixels that have smaller differences in intensity than their neighbors detected but also edge pixels are distinguished from plane pixels. Because the test pixel varies and synchronizes its properties according to the elements in four directions, using directional differences to detect a noisy pixel in stage  $\mathbb{I}$  is very justifiable.

# 2 Experimental Results

The performance of the proposed method was tested under different noise conditions on four test images, as shown in Fig. 2. These are 8-bit gray level images and were all resized to 512 pixel×512 pixel.

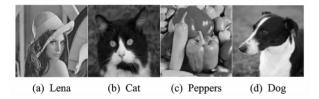


Fig. 2 Test images

The filtering performance of our method was compared with those of median-based filters, including the standard median SM filter (with a  $3\times$ 3 filtering window)[1], CWM filter[9], AMF[1], and the filters proposed by Ebenezer<sup>[24]</sup>, where a directional difference decision-based algorithm with a 3×3 filtering window is applied, Vijayaragavan<sup>[25]</sup>, where directional differences are used to calculate the replacement value with a threshold  $T=0.50\times_{\sigma}$ , Lien<sup>[26]</sup>, which constitutes a decision-tree-based detector with thresholds of 20, 25, 40, 80, 15, and 60, and Turkmen<sup>[27]</sup>, which is a four-phase method with thresholds  $T_1$ ,  $T_2$ ,  $T_3$ ,  $T_4$ ] = [8,15,6,6]. In all the experiments, threshold values  $[T_1, T_2, T_3] = [10, 16, 120]$ were applied in our method. The logic of calculating thresholds directly from noise observation has already been described in Section 1.2.

#### 2.1 Image restoration performance comparison

The test images used in the experiments were contaminated by RVIN with noise ratios ranging from 15% to 75%. A quantitative comparison of the restoration performances of different filters was performed using two image quality evaluation metrics: peak signal to noise ratio (PSNR) and normalized absolute error (NAE)<sup>[1,20-27]</sup>. The PSNR was calculated as

$$PSNR = 10\log_{10}(255^2/MSE)$$
 (7)

Mean square error (MSE) was defined as

$$MSE = 1/MN \sum_{j=1}^{M} \sum_{k=1}^{N} (o_{j,k} - f_{j,k})^{2}$$

where  $o_{j,k}$  and  $f_{j,k}$  represent the original and filtered images of size  $M \times N$ , respectively. A larger value of PSNR reflects a higher quality of the reconstructed image. NAE was calculated as

NAE = 
$$\frac{\sum_{j=1}^{M} \sum_{k=1}^{N} |o_{j,k} - f_{j,k}|}{\sum_{j=1}^{M} \sum_{k=1}^{N} |o_{j,k}|}$$
(8)

A larger NAE value means the quality of the filtered image is poor.

All the experiments were repeated 10 times on each test image corrupted with different noise densities and then the average PSNR and NAE values of the proposed and other comparison filters were calculated, as listed in Table 1. The PSNR and NAE statistics show that SMF, AMF, CWMF, and Ebenezer's method do not give satisfactory results as compared to the other methods. Among the remaining four methods, our method performs fairly well as compared to Turkmen's method, and much better than Vijayaragavan's and Lien's methods. In Turkmen's method, the most similar three neighbors having a chessboard distance equal to two are used as a detector that identifies the corrected pixels as noisy. Therefore, the pixels that are corrected in phase I are changed in phase II, resulting in low PSNR and high NAE values. In contrast, our proposed method corrects only those noisy pixels in stage II that were missed in stage I, and therefore, each noisy pixel is corrected in either stage I or stage [], but not both. Similarly, in Vijayaragavan's method the replacement value is calculated on the basis of pixels in specific directions, and

therefore, the probability that edge pixels are used in the replacement value increases. This results in blurred edges as well as poor filtering.

Table 1 Quantitative results on four test images corrupted with RVIN of different densities

Lena										
_			PSNR					NAE		
Algorithm _		Noise	Density (N	ID)/%		Noise Density (ND)/%				
	15%	30 %	45%	60%	75%	15%	30%	45%	60%	75 %
SMF	32.806	28.019	22.945	18.912	15.901	0.025	0.038	0.069	0.129	0.216
AMF	25.471	20.109	17.019	14.885	13.246	0.026	0.071	0.133	0.211	0.299
CWMF	29.885	25.088	20.717	17.414	14.914	0.037	0.056	0.095	0.162	0.248
Ebenezer	27.467	21.931	18.524	16.014	14.057	0.021	0.054	0.106	0.178	0.268
Vijayaragavan	33.116	28.822	24.722	20.681	16.862	0.014	0.026	0.051	0.095	0.181
Lien	31.085	28.873	25.987	22.178	18.241	0.031	0.038	0.053	0.088	0.163
Turkmen	33.113	30.271	27.554	23.763	19.121	0.012	0.021	0.034	0.062	0.134
Proposed method	33.922	31.284	27.865	23.931	19.522	0.011	0.019	0.033	0.061	0.129
Peppers										
SMF	36.533	28.731	22.721	18.431	15.321	0.011	0.025	0.061	0.129	0.231
AMF	24.856	19.282	16.267	14.103	12.475	0.023	0.074	0.145	0.233	0.333
CWMF	32.957	26.373	21.289	17.532	14.768	0.022	0.038	0.079	0.152	0.251
Ebenezer	26.671	21.008	17.745	15.295	13.358	0.017	0.055	0.113	0.194	0.295
Vijayaragavan	36.692	30.062	25.078	20.622	16.524	0.007	0.019	0.042	0.091	0.184
Lien	35.536	31.472	27.379	22.545	17.886	0.015	0.022	0.037	0.077	0.168
Turkmen	37.151	32.768	28.914	25.047	19.186	0.006	0.013	0.024	0.047	0.128
Proposed method	37.353	32.953	29.222	24.833	19.732	0.005	0.012	0.023	0.048	0.126
Cat										
SMF	37.413	27.045	20.381	15.891	12.902	0.016	0.048	0.144	0.333	0.588
AMF	22.975	17.569	14.532	12.352	10.744	0.051	0.163	0.321	0.521	0.739
CWMF	32.702	23.655	18.019	14.276	11.743	0.031	0.087	0.225	0.447	0.711
Ebenezer	24.968	19.265	15.906	13.356	11.444	0.036	0.121	0.257	0.453	0.686
Vijayaragavan	36.431	29.076	23.384	18.379	14.058	0.011	0.035	0.091	0.215	0.468
Lien	37.709	33.274	27.539	21.255	15.459	0.021	0.031	0.061	0.016	0.433
Turkmen	40.409	36.256	33.028	26.021	17.236	0.006	0.014	0.023	0.069	0.333
Proposed method	40.746	36.899	30.812	25.898	17.819	0.006	0.014	0.032	0.071	0.325
Dog										
SMF	38.271	27.601	20.674	16.292	13.323	0.007	0.023	0.076	0.178	0.317
AMF	23.318	17.844	14.725	12.576	10.967	0.027	0.092	0.184	0.299	0.425
CWMF	34.392	25.205	19.271	15.449	12.749	0.013	0.037	0.101	0.209	0.346
Ebenezer	24.798	19.307	16.059	13.592	11.711	0.023	0.072	0.152	0.261	0.387
Vijayaragavan	37.451	29.441	23.689	18.765	14.425	0.005	0.018	0.048	0.116	0.253
Lien	39.157	33.372	27.304	21.282	15.518	0.009	0.015	0.032	0.089	0.245
Turkmen	41.031	35.231	31.113	25.078	17.372	0.003	0.008	0.018	0.041	0.185
Proposed method	40.984	35.809	30.842	25.447	18.391	0.003	0.007	0.018	0.039	0.177

#### 2. 2 Processing time

A comparison of the processing time of the proposed and other baseline filters is given in Table 2. SMF, AMF, CWMF, and Ebenezer's method are faster but yield worse results than the other three methods. Lien and Turkmen's meth-

ods are slower than all the baseline methods. The reason for this is that the image is scanned four times and a variable sized window is used in Turkmen's method, while many variables are calculated in Lien's method. The proposed algorithm is faster than Vijayaragavan, Lien, and

Turkmen's methods because of its single scan and fixed window size design. The proposed and other comparison filters were implemented using MAT-LAB R2013a. All the experiments were performed on a Win7-PC with Intel(R) Core(TM) i5-3320M, CPU 2.6 GHz.

Table 2 De-noising time in seconds for Peppers image

Algorithm -	ND								
Algorithm	15%	30 %	45%	60%	75%				
SMF	3.16	2.67	6.60	6.22	3.86				
AMF	5.46	4.41	12.00	13.57	7.61				
CWMF	3.02	2.75	7.49	8.54	4.85				
Ebenezer	3.20	3.01	6.30	8.87	6.25				
Vijayaragavan	20.49	15.22	34.19	37.54	27.61				
Lien	47.72	44.45	40.71	39.31	43.64				
Turkmen	39.22	51.67	47.54	45.91	48.46				
Proposed	11.54	11.07	22.57	25.33	15.30				

## 2.3 Comparison of visual performance

All the test images were corrupted with different noise densities and filtered using different methods, as shown in Figs. 3, 4, respectively. The visual results show that SMF performs well in terms of filtering noises having a low density, but is not effective when applied to images having high noisy densities. The output images of AMF, CWMF, and Ebenezer's method are very similar to each other and do not outperform SMF. However, Vijayaragavan, Lien, and Turkmen's methods yield a significantly better visual performance. Among these three, Lien's method preserves edges more efficiently than Turkmen's method, which effectively filters noise. In contrast, our method shows a similar performance at first glance, but closer observation reveals that it outperforms all the other compared methods in terms of both noise removal and fine detail preservation, as shown in Fig. 5. The boundary lines of the dog's nose in Dog can be seen clearly in the image filtered by our method, whereas in those filtered by other methods the nose edges remain blurred with some corrupt blotches. Similarly, the nose and lips in Lena and the nose edges of the cat in Cat are sharper and better distinguished in the images filtered by the proposed method. Therefore, our method is efficient in terms of edge preservation. The four-phased methodology of Turkmen confuses edge and plane surface noisy pixels, and thus, pixels at sharp edges receive values similar to those of plane surface pixels, which results in blurred edges. The isolation module in Lien's method affects the filtering performance. Similarly, when the edge pixels are used in the calculation of replacement values in Vijayaragavan's method, the edges are expanded toward the plane surface, which renders noisy and edge pixels indistinguishable. As the intensity values of the noisy pixels are random and the number of pixels similar to a noisy pixel is changed randomly, it is appropriate to examine the noisy pixels twice, as in the proposed method. In our method, obvious noise is corrected at stage I and missed noisy pixels are rectified at stage II, and therefore, two different replacement values calculated by different methods are used, which enhance the proficiency of edge protection. Thus, the proposed method exhibits the best visual performance with the preservation of trivial details.



(a) Lena (30%) (b) Cat (45%) (c) Peppers (60%) (d) Dog (75%)

Fig. 3 Noisy images with different noise ratios

#### 2. 4 Selection of threshold parameters

Three threshold parameters,  $T_1$ ,  $T_2$ , and  $T_3$ , were used in our experiments. The values of parameters usually influence the results significantly. In this subsection, we describe three sets of experiments conducted to show that  $[T_1, T_2, T_3] = [10,16,120]$  are the best parameters that can be used in image de-noising experiments. These three sets of experiments were all performed on the Lena image. In each set of experiments, the values of two parameters were fixed while the value of the remaining parameter was varied. The PSNR results of this series of experiments are plotted in a curve in Fig. 6. First, we

set the values of parameters  $T_2$  and  $T_3$  to be 16 and 120, respectively, to analyze the influence of  $T_1$  on the filtering performance. It is obvious from the graph of  $T_1$  that the PSNR value increases as the threshold increases until it reaches an optimum PSNR value and then decreases again with a further increase in  $T_1$ . Threshold  $T_1$  gives the best results in the range [8,12] and the optimum threshold is approximately 10. Second, we

fixed  $T_1$  and  $T_3$  at values 10 and 120, respectively, to determine the effect of  $T_2$  on the PSNR value. Threshold  $T_2$  yields the best performance in the range [13, 20] and the maximum PSNR value is obtained at  $T_2 = 16$ . Third, for threshold  $T_3$  our method performs well in the range [117, 123], when the values of  $T_1$  and  $T_2$  are fixed at 10 and 16, respectively. The highest PSNR value is attained at  $T_3 = 120$ .

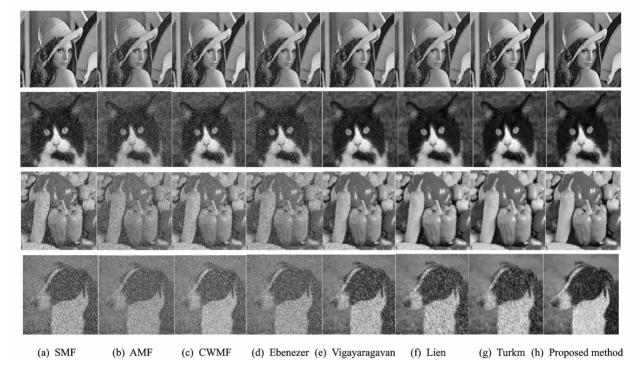


Fig. 4 Visual results for restoring Lena, Cat, Peppers, and Dog corrupt images with noise ratios of 30%, 45%, 60%, and 75%, respectively

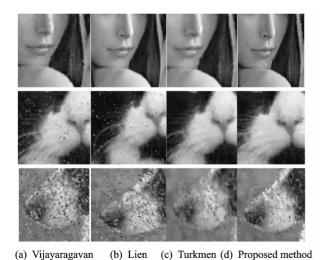


Fig. 5 Edge preservation results for restoring Lena, Cat, and Dog corrupt images with noise ratios of 15%, 45%, and 75%, respectively

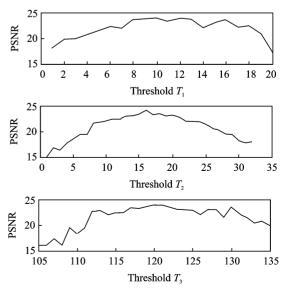


Fig. 6 Dependence of PSNR on parameters  $T_{\rm 1}$  ,  $T_{\rm 2}$  and  $T_{\rm 3}$  for Lena image

## 3 Conclusions

In this paper, a two-staged nonlinear filtering algorithm was proposed. In the first stage of our method, noisy pixels are detected using nearest neighbors, while in the second stage noisy pixels are detected using directional differences. The replacement value in stage I is calculated using the median value of all neighboring pixels, except the first most similar one, whereas the median value of elements in specific directions is used to calculate the replacement value in stage []. The proposed algorithm was tested on images contaminated with different noise densities. The experimental results disclose that the proposed method exhibits a better performance than other methods in terms of both noise removal and processing time. Furthermore, because of the dual check of a noisy pixel in two cascaded stages, our method outperforms all other comparison methods in terms of edge and minor detail preservation. To summarize, our method is efficient in terms of processing time, noise removal, graphic appearance, and edge preservation. Future work will focus on improving the proposed method to make it appropriate for processing the color images and removing other types of noise.

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