

Sectorization Model of Terminal Airspace with Arrival and Departure Separation

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(Received 18 November 2014; revised 2 January 2015; accepted 12 January 2015)

Abstract: Terminal airspace (TMA) is the airspace centering several military and civil aviation airports with complex route structure, limited airspace resources, traffic flow, difficult management and considerable airspace complexity. A scientific and rational sectorization of TMA can optimize airspace resources, and sufficiently utilize the control of human resources to ensure the safety of TMA. The functional sectorization model was established based on the route structure of arriving and departing aircraft as well as controlling requirements. Based on principles of sectorization and topological relations within a network, the arrival and departure sectorization model was established, using tree based ant colony algorithm (ACO) searching. Shanghai TMA was taken as an example to be sectorized, and the result showed that this model was superior to traditional ones when arrival and departure routes were separated at dense airport terminal airspace.

Key words: air traffic management; arrival and departure sectorization model; controller's workload; route structure of arriving and departing aircraft; Ant colony algorithm

CLC number: V355.2

Document code: A

Article ID: 1005-1120(2016)04-0442-09

0 Introduction

With the rapid development of air transport industry, air traffic flow is constantly roaring, and limited airspace resource has become the bottleneck of air traffic growth. Olaf et al. estimated^[1] that the global air transport volume would reach three times of it now in 2025. Thus, it is pressing to upgrade the capacity of the air transportation system. Single European Sky ATM Research (SESAR)^[1] and the U. S. Next Generation Air Transportation System (Next-Gen)^[2] came up with the idea of establishing the next generation air transportation system in the coming 10 to 15 years. In this process, the effective management of air traffic resource is a key aspect. Terminal airspace (TMA) is an airspace centering the medium and low airspaces of several military and civil aviation airports with complex route structures, limited airspace resources, traffic flow, difficult management and considerable

airspace complexity. A scientific and rational sectorization of TMA can optimize airspace resources, and sufficiently utilize the control of human resources to ensure the safety of TMA, thus improving the air traffic service capacity.

The theory and method of airspace sectorization has become the focus of airspace planning and management. In recent years, experts in this field have further underscored the mathematical models and algorithm to determine the sectorization plan, including graph theory, genetic algorithm and the design of computational geometry. Existing studies highlighted two-dimensional airspace^[3-16]; Delahaye et al.^[3] proposed the sectorization design based on genetic algorithm and computational geometry. Firstly, the method quantified the workload during control operation. Then, Voronoi algorithm of computational geometry was applied to the two-dimensional blocking of random airspace joints. Each Voronoi polygon

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contained different workloads. Eventually, with the optimization criteria of balanced workload, the sectorization goal could be met through genetic algorithm. Yet, as the method mainly used in randomly generated joints and chose the airspace for free flight as research background, it is not adequate for fixed route structure of existing airspaces. In addition, the research is confined in the two-dimensional airspace. Yousefi et al. [4-5] put forward a sector optimization method based on the workload of the controller. Firstly, they analyzed the acknowledging workload of controllers and the analysis model of airspace complexity. Next, according to the operating altitude scope, the national airspace of America was divided into three layers as low altitude, high altitude and super altitude. Each layer could be further divided into 2 566 hexagons, each of which had a side length of 24 nautical miles. Hexagons compromised the basic design unit of the airspace. Next, the temporal and spatial distribution of workloads in the airspace and terminal area was identified to acquire the crowded period of time of national airspace of America. Ultimately, the clustering algorithm of optimization theory was applied to the combination of hexagon groups to divide the controlling center and sector boundary of the U. S. national airspace. Compared with the study of Delahaye, this study also took the perspective of basic design unit and controllers' workloads, while holding better practical values. However, this study still limited in three aspects: The study targeted at the en-route control area, failing to refer to TMA ; with the consideration of the operative convenience of controllers, this study ignored dynamic sectorization; in addition, key limitation conditions such as the design of conflict points were not considered in this study. On the basis of the above mentioned research, scholars from Europe and America conducted consecutive studies on this. For example, Verlhac et al. [6] proposed a integer design technique; D. Gianazza et al. [7] developed a tree search algorithm. Huy Trandac et al. [8] proposed a constraining design method of airspace sector. Davide Famanelli et al. [9] intro-

duced the graph theory to the optimization of airspace. The existing research findings [10-16] have laid valuable foundation for our research.

In TMA segment design, the sectorization was conducted according to the arrival and departure function of aircraft [17]. Meanwhile, the vertical interval between the arrival and the departure routes was drawn out to ensure security. Controllers' command can line up aircraft arrived from corridor entrance, which are directly handed over to the final of the airport. Departure aircraft are directly handed over to adjacent regions through departure control. Currently, in the sectorization based on geographical regions, a complete arrival and departure route is often divided into an array of sectors, generating extra control transferring workloads between sectors. Thus, according to the arrival and departure function of aircraft, the sectorization can keep the relevant coordination to the lowest level, and maintain the climbing performance of departure aircrafts close to the optimum level, thus ensuring the orderly safe arrival and departure. The approach is especially necessary for complex TMA with multiple airports (such as Shanghai TMA) because it can effectively avoid frequent transfer and coordination of arrival and departure flows among different airports, which greatly alleviates workloads of control and flight. Although sectorization has been applied to those international terminal areas with considerable traffic density, most existing approaches used qualitative design, which fails to provide efficiency and accuracy for sectorizing dense terminal areas of airports. Therefore, we established arrival and departure sectorization model considering arrival and departure separation.

1 Arrival/Departure Sectorization Model

1.1 Route of controller workloads

Typically, controllers' workload can be described as: The airspace is divided into a number of sectors, each of which is assigned to a group of

controllers. Controllers of each sector are required to complete the monitoring of flights to avoid conflicts among aircraft, and to exchange information with adjacent sectors in the planned routes of aircraft. These tasks can be divided into three parts: Supervision workload, conflict workload and coordination workload.

Workloads of controlling command are mapped to the routes. The route network can be expressed as a weighted graph $\mathbf{G}=(\mathbf{V}, \mathbf{E})$, where \mathbf{V} is the set of vertices, that is, the set of navigation stations and intersection points u ; \mathbf{E} the set of sides. In addition, when and only when a straight route exists from u to v , $(u, v) \in \mathbf{E}$, the controlling workloads on the routes can be expressed as

$$\omega_e = \left(c_u + \frac{m_e}{2}\right) + \left(c_v + \frac{m_e}{2}\right) + o_e \quad (1)$$

where, ω_e is the weight of controlling workloads of route e ; c_u, c_v are conflict workloads rising from the conflicts of u and v ; m_e the monitoring workloads, belonging to a side $e=(u, v)$, and it has been divided into two equal parts $m_u=m_v=m_e/2$, which are assigned to u and v ; o_e the coordination workloads, which are assigned to side e . If the vertices of a side fall in one sector, $o_e=0$. The load weights of $V-E$ on the route then can be calculated. Therefore, each route can be set as a finite element, and has a weight of controlling workloads.

1.2 Distribution of controller workloads in airspace

On the basis of airspace traffic flow prediction and historical data of TMA workloads, TMA controlling workloads can be distributed according to Cancning schedule of the controlling command, and then mapped to the three-dimensional terminal airspace route network. Therefore, the distribution of workloads in the route network is determined. We also presented a centroid method of controlling workloads as follows.

In order to illustrate the airspace distribution of controlling workloads, the regional distribution of controlling workloads can be concentrated on a centroid point, that is, the centroid of con-

trolling load unit. In accordance with the weight distribution in physics, the centroid can be identified as the center-of-gravity position of controlling workloads.

Assume that the controlling load finite element i obtains N controlling load points, and the j controlling load point is presented as (x_j, y_j) , so that the centroid is

$$\begin{cases} X_i = \sum_{j=0}^N x_j / N \\ Y_i = \sum_{j=0}^N Y_j / N \end{cases} \quad (2)$$

Through the acquiring raw data of flight flow distribution the airspace distribution of controlling workload centroid is identified.

1.3 Topological presentation of route network

If the computer is used in the TMA optimized sectorization, data collection of controller workloads and mathematical description of TMA structure on the route should be accomplished first so that the topological relationship matrix among the route finite elements can be built up.

A route that connected nodes, like navigation stations, the airports and position reporting points can be divided into a limited number of routes. A route is the basic finite element of optimized sectorization, and the topological relationship matrix among the route finite elements can be established. Straight routes of routes in TMA are expressed by the set $\mathbf{R}=[r_1, r_2, \dots, r_n]^T$, and the topological matrix among routes in the airspace can be expressed as

$$\mathbf{G} = \begin{bmatrix} g_{11} & g_{12} & \cdots & g_{1n} \\ g_{21} & g_{22} & \cdots & g_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ g_{n1} & g_{n2} & \cdots & g_{nn} \end{bmatrix} \quad (3)$$

where the elements of matrix \mathbf{G} have $g_{ij} \in \{0, 1\}$. $g_{ij}=1$ shows the correlation between route i and route j ; $g_{ij}=0$ shows the irrelevance of i and j ; n is the route number in TMA serving as the basic finite elements for the optimizing search of sectorization.

1.4 Calculation model of sector number

According to the DORATASK method rec-

ommended by ICAO^[18], the average workloads of controllers should be less than 80% of the time statistics. Based on this principle, it should be ensured that the total workloads in the airspace is minimized. Firstly, the total workloads W_T of controlling in the airspace should be collected and N_s , the number of divided sectors should meet the following equations

$$N_s = \begin{cases} \text{int}M + 1 & M \neq \text{int}M \\ \text{int}M & M = \text{int}M \end{cases} \quad (4)$$

$$M = \frac{W_T}{S \times 80\%} \quad (5)$$

where S is the statistical time of sector; and int the rounding function; N_s the minimum number of sectors. W_T is the total airspace workloads, which is expressed by time. When the result of M is not an integer, the calculation results should be rounded plus 1 to reach N_s ; if M is an integer, N_s is directly obtained.

1.5 Sector optimization target model

The bi-level optimization model of sectors is built under the premise of the estimated minimum number of sectors. The target is to achieve the sector load balance under the premise of the minimum total load in TMA. The following model was thus built up

$$J = \min \left(\sum_i^s \omega_{ci} + \sum_j^{N_s} \omega_{vj} \right) \quad (6)$$

where ω_{ci} is the fixed load on i , including monitoring loads and coordination loads; ω_{vj} the transferred load of sectors; s the number of finite element divided in the airspace.

On the basis of the model which ensured the minimum load of TMA, the secondary target of sector optimization is to meet the balance of controller's workloads among all sectors

$$J' = \min \sum_{k=1}^{N_s} |\omega_k - \mu| \quad (7)$$

where ω_k is the workload of the k sector and μ is the average load of N_s sectors.

In the actual division of the sectors, in addition to the impact of capacity and load, we should also consider the actual controlling states and airspace rules so that the following optimization constraints should be introduced in the operation.

Let each flight be i , and the ordered list of the route vertexes in the flight plan can be expressed as $(v_1^i, v_2^i, \dots, v_{pi}^i)$.

(1) Functional constraints of sectors

In order to acquire the functional uniformity of route finite element in each sector, functional constraints of sectors should be included, which can be illustrated by the conflicts in finite elements and nature of controlling commands. Generally, a sector can hold the same arrival controlling or departure controlling, so as to maximize the reduction of coordination loads.

For Route R_{pk}^i , i is the route of TMA, $i \in \{1, 2, \dots, n\}$; p the property of arrival and departure, $p \in \{0, 1\}$, $p=1$ shows that the flight is arriving and $p=0$ the flight is departing; k the airport property, $k \in \{1, 2, \dots, a\}$. TMA involves many airports. During the finite element search with sector capacity conditions, if R_{pk}^i and $R_{p'k'}^j$ belong to sector S_i , two search priorities should be satisfied; First, to ensure that the same route property of the same airport is separated to one sector, i. e. $k=k'$ and $p=p'$; second, to separate the same route property of different arrivals to one sector, i. e. $p=p'$ and $k \neq k'$.

(2) Minimum sector crossing time constraints

To ensure the operation margin of deployment and instructions of the air controllers (Fig. 1), aircraft should stay in the sector longer than the set minimum time duration, i. e. T_{\min} . T_{\min} value should be two times of ω_c , the time of the transfer of instruction, i. e.

$$T_c \geq T_{\min} = 2 \times \omega_c \quad (8)$$

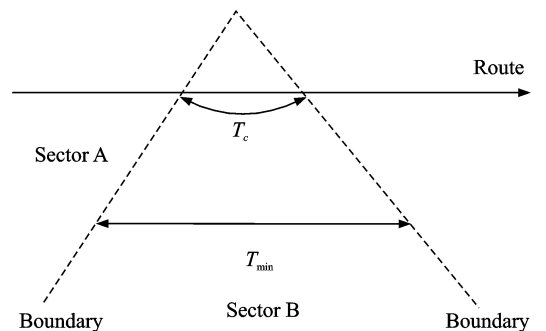


Fig. 1 Minimum sector crossing time constraints

(3) Minimum distance constraints of the sector boundary rendezvous points (the intersections)

The distance of the sector boundary rendezvous points must be longer than a given value, which can provide sufficient time for controllers to deal with conflicts at nodes, so as to prevent aircraft of other sectors from entering the nodes and therefore avoid new conflicts (Fig. 2).

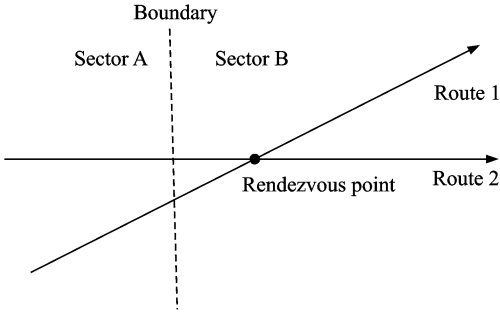


Fig. 2 Minimum distance constraints of the sector boundary rendezvous points (the intersections)

Set required time of controllers to solve the conflict at the nodes as ω_f , the transfer time of sector as ω_c , aircraft interval as ω_j , and the minimum time for the sector boundary and nodes is

$$T_h \geq \omega_f + \omega_c + \omega_j \quad (9)$$

(4) Convex constrains

In order to reduce the substantial coordination workloads from frequent crossing flights, a flight should not cross the same sector for several times (Fig. 3). Hence, for all planned flights I and the sector of way points on the same route x_a^i, x_b^i, x_c^i , if the time order is $a < b < c$, and x_a^i and x_c^i are in the same sector, it can be inferred that x_b^i is in this sector: $\forall i, \forall a < b < c: x_a^i = x_c^i \Rightarrow x_a^i = x_b^i$.

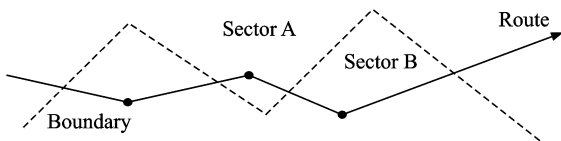


Fig. 3 Convex constrains of sectors

1.6 Sectorization optimization algorithm

Ant colony algorithm is completed in following steps.

Step 1 Initialize the route finite element

properties in TMA. Set arrival as 1, departure and combined arrival and departure as 0. The load value of each finite element is acquired from the investigation data, and the initial transfer intensity and visibility of each unit is set.

Step 2 Select the initial search finite element. For internal and external sectors, the last approaching finite element is taken as the initial unit. For those with busy routes as the center, the corridor entrance finite element can be selected. The property of this entrance finite element is 1 to form the initial sector.

Step 3 For Ant i in Group j , the sub-unit correlated with current sector can be selected. If correlated, the query Table A is stored to calculate the transfer probability of each unit. According to the probability interval, the entering unit can be selected. Meanwhile, the cumulative strength of the transfer of the finite element can be updated. If $i=n$ (when ants of this group finish the query, and transfer intensity is transferred), the cumulative intensity is assigned to the transfer intensity of the unit.

Step 4 Collect the loads of sectors. If the load meets $W_i \leq S \times 80\%$, go to Step 5. If not, go to Step 3.

Step 5 Determine the target function. If improved, the combination is recorded, other wise the previous record is maintained.

Step 6 Output the eventually optimized target function and combination of controlling load.

2 Analysis of Examples

2.1 Route load statistics of Shanghai TMA

Based on the real-time radar voice data of Shanghai TMA and the controlling instruction distribution range, all arriving flights of Shanghai TMA were divided into four states: Initial contact, control altitude, waiting or motor deployment and control speed. Similarly, all departure flights were divided into three states: Initial contact, control altitude and departure transfer. Through navigation stations, airports, location report spots and so on, routes were divided into finite element and numbered. The entire route of

instructions, as well as the statistic analysis of controller workloads in this sector. The data was reasonably inferred from the actual condition of Shanghai TMA. In addition, through the access to the finite element database and airspace controlling load database, we collected the controller's workload on each unit. The ant colony algorithm was used for optimized search.

According to Eqs. (4), (5), the aircraft controlling workloads (without considering the loads of east-west Pudong sectors) were substituted, where $W_T=10\ 567\ s$ and $S=3\ 600\ s$, and we obtained that $N_s=4$. In other words, the minimum sector number was 4.

In the optimized sectorization model, ant colony algorithm was used to optimize this model and combine the finite element according to the functional uniformity. The sectorization result is shown in Table 3.

As the sector was expanded from the finite element to the airspace, the qualitative design ensured the safety interval of departure routes and the protection range of intersections. Therefore, final optimized sectorization was achieved. Fig. 5 shows the three dimensional graphs of 6 functional sectors with NX7.0 CAD.

2.3 Analysis on Shanghai TMA micro-simulation system

For the two plans of sectorization, 30 groups of flow data in peak hours in the design year were simulated. The simulation results were statistically analyzed (Table 4).

Simulation and analysis indicators of TMA air traffic micro-simulation system (Fig. 6) were hourly controller workloads, that is, workloads

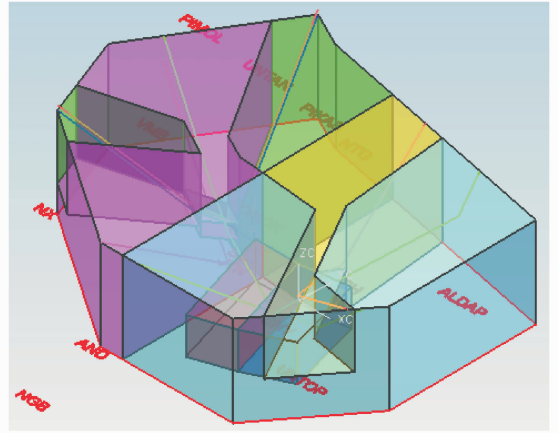


Fig. 5 The space diagram of north orientation sectorization of Shanghai TMA

of air traffic controlling in an hour for one controller. We analyzed whether loads in each sector meet the controller workloads defined in DO-RATASK. The north orientation arrival of Shanghai TMA was taken as an example to simulate the peak hour flow of future plans of sectorization, and the results were analyzed statistically.

Plan A applied regional functional sectorization and Plan B utilized the traditional geographic sectorization. Plan A divided TMA into 6 sectors (including 2 sectors of east-west entrances of Pudong Area). Plan B divided TMA into 7 sectors. For the two plans, 30 groups of peak hour flow data in 2012 were simulated, and the average controller workloads of each sector are shown as follows.

Table 4 shows that Plan B achieved uniform load distribution and the total load of Plan B was larger than that of Plan A. Controller workloads

Table 3 Departure sector load distribution after optimized sectorization

Sector name	01 sector (HQ arrival sector)	02 sector (HQ departure sector)	03 sector (PD arrival sector)	04 sector (PD departure sector)
Finite element	1, 7, 8, 9, 11	13, 14, 16, 19, 20	0, 2, 3, 4, 5, 6, 10	12, 15, 17, 18, 21, 22, 23, 24, 25
Total loads /s	2 416	2 125	2 547	2 396

Table 4 Comparison of two plans of hourly peak controller workload of each sector in 2012

Sector number	01	02	03	04	05	06	07	Total
Plan A	2 416	2 125	2 747	2 396	2 299	2 229		14 212
Plan B	2 689	2 541	2 789	2 631	2 308	2 366	2 655	17 979

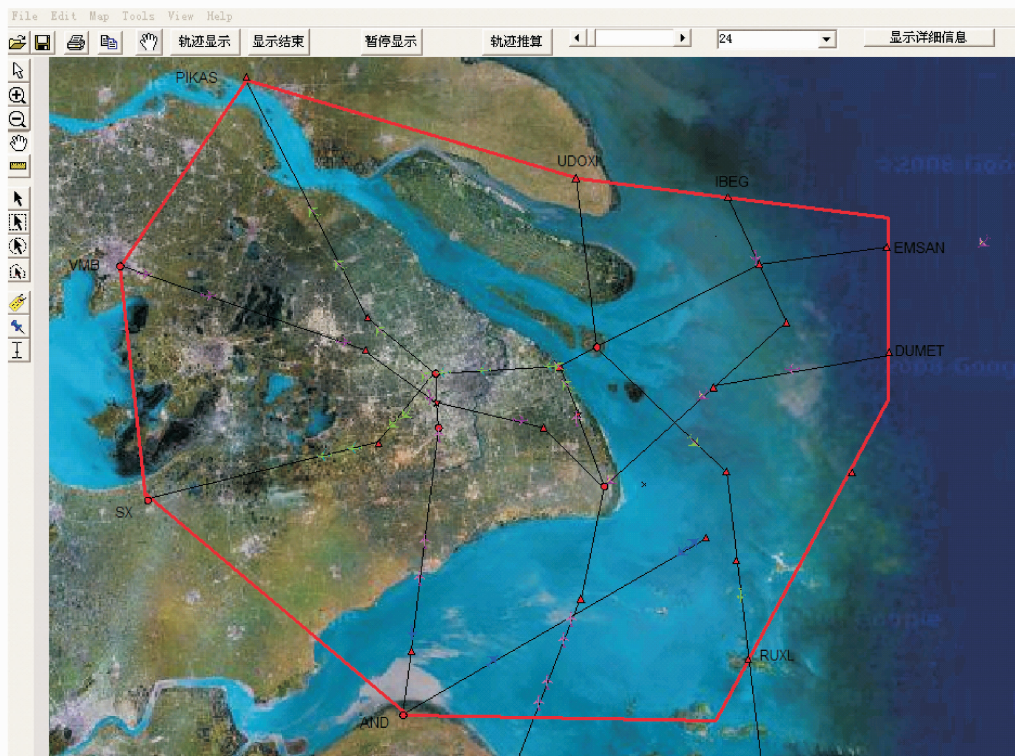


Fig. 6 Shanghai TMA micro-simulation system

of each sector in the two plans were less than 2 880 s, which met the controller workloads as defined in DORATASK. Thus, the operation workloads were greatly improved for controllers.

Therefore, comparison between the two sectorization plans in terms of airspace performance indicators showed that although functional sectorization could not optimize the balance of sector loads, it could effectively reduce the controlling airspace difficulty, as well as the coordination workloads. Thereby, it reduced the workloads of the entire airspace, expanded the airspace capacity, and optimized the operating environment of airspace. Hence, the sectorization with the separation of arrival and departure efficiently alleviated the pressure imposed by limited airspace resources, presenting outstanding advantages for the sectorization of TMA with frequent flight conflicts.

3 Conclusions

The functional sectorization model is established based on the characteristics of the route

structure of separated arriving and departing aircraft as well as the operation requirements of controlling. The quantitative, simulation and comparative study illustrated that the functional design of airspace sector outweighed the geographic design by reducing controller workloads and airspace delay. In this study, tree theory of airspace delay was used in the sectorization of the arrival and departure separation. Based on constraints of sectorization and topological relations in the network, the ACO search was used to establish the arrival and departure sectorization model. The quantitative results were achieved.

In future research, the dynamic sectorization of TMA with the complex air traffic and climates would be the focus.

Acknowledgements

This work was supported by the National Natural Science Foundation of China (Nos. U1233101, 71271113) and the Fundamental Research Funds for the Central Universities (No. NS2016062).

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