# Numerical Simulation of ATPS Parachute Transient Dynamics Using Fluid-Structure Interaction Method

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Abstract: In order to simulate and analyze the dynamic characteristics of the parachute from advanced tactical parachute system (ATPS), a nonlinear finite element algorithm and a preconditioning finite volume method are employed and developed to construct three dimensional parachute fluid-structure interaction (FSI) model. Parachute fabric material is represented by membrane-cable elements, and geometrical nonlinear algorithm is employed with wrinkling technique embedded to simulate the large deformations of parachute structure by applying the Newton-Raphson iteration method. On the other hand, the time-dependent flow surrounding parachute canopy is simulated using preconditioned lower-upper symmetric Gauss-Seidel (LU-SGS) method. The pseudo solid dynamic mesh algorithm is employed to update the flow-field mesh based on the complex and arbitrary motion of parachute canopy. Due to the large amount of computation during the FSI simulation, massage passing interface(MPI) parallel computation technique is used for all those three modules to improve the performance of the FSI code. The FSI method is tested to simulate one kind of ATPS parachutes to predict the parachute configuration and anticipate the parachute descent speeds. The comparison of results between the proposed method and those in literatures demonstrates the method to be a useful tool for parachute designers.

**Key words:** parachute dynamics; fluid-structure interaction; nonlinear structure dynamics; time dependent flow; parallel computation technique

#### 0 Introduction

Although parachute system is the most useful air-dropping device, it brings many challenges for both experimental test and numerical simulation<sup>[1]</sup>. Moreover, the modern combat-ready airborne troops are usually equipped with heavier tactical weapons and need more slowly impact speed at the end of parachute landing procedure. Designing new parachute configurations such as advanced tactical parachute system (ATPS) parachute program will need more convenient numerical method to predict and evaluate parachute dynamic characteristics.

One kind of parachute fluid-structure interaction (FSI) method uses mass-spring damper (MSD) model to treat the parachute as a virtual spring net. Although this spring model can provide basic parachute profiles<sup>[2-5]</sup> or shapes<sup>[6]</sup> for fluid computation, it is still difficult to simulate complex new parachute configurations especially when the strings go through the fabric canopy. The other kind of parachute FSI method is the deforming-spatial-domain/stabilized space-time (DSD/SST) formulation<sup>[7-13]</sup> which is based on finite element method. However, using finite element method to solve flow problem can be very time-consuming and need extra technique to solve compressible flow problems. The last kind of parachute FSI method is using commercial software<sup>[14-15]</sup>, but they usually use explicit iteration method which can severely limit time step.

A FORTRAN code containing three modules is developed within massage passing interface

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(MPI) parallel environment in this paper to conduct the FSI simulation of ATPS parachute problems. The three modules are implicit nonlinear finite element structure solver, preconditioned unsteady flow solver and pseudo solid dynamic mesh solver, respectively. The FSI method combines the implicit nonlinear structure dynamic algorithm with the unsteady preconditioning method for the first time to predict ATPS parachute dynamic characteristics. The simulation results agree with Ref. [1], which demonstrates its ability in helping design new parachute configurations.

## 1 Nonlinear Structure Dynamic Model

#### 1.1 Governing equation for structure model

The nonlinear structure dynamic formula for membrane-cable system can be established by applying total Lagrangian scheme with incremental/iteration method<sup>[16, 17]</sup>

$$\mathbf{M} \bullet_{k+1}^{t+\Delta t} \ddot{\mathbf{U}} + \mathbf{C} \bullet_{k+1}^{t+\Delta t} \dot{\mathbf{U}} +_{k}^{t+\Delta t} \mathbf{K}_{\mathrm{T}} \bullet$$

$$\begin{bmatrix} t+\Delta t \\ k+1 \end{bmatrix} \mathbf{U} -_{k}^{t+\Delta t} \mathbf{U} \end{bmatrix} \stackrel{+}{=}_{k+1}^{t+\Delta t} \mathbf{F} -_{k}^{t+\Delta t} \mathbf{R} \tag{1}$$

where M, C,  $K_T$  and U are consistent mass matrix, mass damping matrix, tangent stiffness matrix, global displacements vector, respectively. F and R are the pressure loading and the restoring force, respectively. The superscript t represents structural time step and the corresponding subscript k the Newton-Raphson iteration number. The second Piola-Kirchoff stress tensor  $S^{a\beta}$  and Green-Lagrange strain tensor  $E^{a\gamma}$  are employed to describe the geometrical nonlinear deformation system based on the fourth-order elastic tensor  $C_{a\beta}$ 

$$\mathbf{S}^{\alpha\beta} = \mathbf{C}_{\alpha\beta\xi\eta} \mathbf{E}^{\xi\eta} \tag{2}$$

The membrane tangent stiffness matrix K for nonlinear structural simulation is [17]

$$^{t+\Delta t}\boldsymbol{K}_{N_{i}M_{j}} = \frac{1}{2}\delta_{ij}\boldsymbol{S}^{a\beta}\left(H_{N,a}H_{M,\beta} + H_{M,a}H_{N,\beta}\right)h\sqrt{\boldsymbol{G}} + \frac{1}{4}\boldsymbol{C}_{a\beta\xi\eta} \cdot (H_{N,a}H_{L,\beta} + H_{L,a}H_{N,\beta}) \cdot (X_{Li} +_{k}^{t+\Delta t}\boldsymbol{U}_{Li})\left(H_{M,\xi}H_{Q,\eta} + H_{Q,\xi}H_{M,\eta}\right)\left(X_{Qj} +_{k}^{t+\Delta t}\boldsymbol{U}_{Qj}\right) \cdot h\sqrt{\boldsymbol{G}} \tag{3}$$
 where  $\boldsymbol{G}$  is the metric tensor;  $h$  the membrane thickness;  $\delta$  the Kronecker symbol.  $N, M, L, Q$  are the local node index of one element;  $i, j$  the three directions of Cartesian coordinates; Capital

letter X and H the Cartesian coordinates and interpolation shape function, respectively. Similarly, the tangent stiffness matrix for the nonlinear cable elements is ( $A_s$  represents cable cross-sectional area)

$$E^{t+\Delta t} \mathbf{K}_{N_{i}M_{j}} = \delta_{ij} \mathbf{S}^{11} H_{N,1} H_{M,1} A_{s} \sqrt{\mathbf{G}} + EA^{11} A^{11} H_{N,1} H_{L,1} \cdot (X_{L_{i}} +_{k}^{t+\Delta t} U_{L_{i}}) \cdot H_{M,1} H_{Q,1} \cdot (X_{Q_{j}} +_{k}^{t+\Delta t} U_{Q_{j}}) A_{s} \sqrt{\mathbf{G}}$$
(4

It should be noticed that the membrane wrinkling algorithm in Ref. [18] is employed in this paper to eliminate the compression stress in the membrane elements, which can simulate the fabric special wrinkling phenomenon and improve the numerical stability.

#### 1.2 Structural time-integration formulation

By applying the implicit Newmark time integration scheme<sup>[17]</sup>, the structural dynamic equation at time level  $t+\Delta t$  with nonlinear Newton-Raphson iteration step number k is

$$\begin{bmatrix}
t^{+\Delta t} \mathbf{K}_{\mathrm{T}} + \frac{M}{\beta \Delta t^{2}} + \frac{\alpha}{\beta \Delta t} \mathbf{C} \end{bmatrix} \begin{bmatrix} t^{+\Delta t} \mathbf{U} - t^{t} \mathbf{U} \end{bmatrix} = \\
t^{+\Delta t} \mathbf{F} - t^{+\Delta t} \mathbf{R} - \mathbf{M} \cdot \left\{ \frac{1}{\beta \Delta t^{2}} \begin{bmatrix} t^{+\Delta t} \mathbf{U} - t^{t} \mathbf{U} \end{bmatrix} - t^{t} \mathbf{U} \right\} - \\
\frac{\dot{\mathbf{U}}}{\beta \Delta t} - \left( \frac{1}{2\beta} - 1 \right) \cdot \dot{\mathbf{U}} - \mathbf{C} \cdot \left\{ \left( 1 - \frac{\alpha}{\beta} \right) \cdot t^{t} \mathbf{U} \right\} - \\
t^{t} \mathbf{U} + \Delta t \left( 1 - \frac{\alpha}{2\beta} \right) \cdot \dot{\mathbf{U}} + \frac{\alpha}{\beta \Delta t} \begin{bmatrix} t^{+\Delta t} \mathbf{U} - t^{t} \mathbf{U} \end{bmatrix} \right\} (5)$$

where  $\alpha$  and  $\beta$  are chosen as 0.500 and 0.250, respectively. The generalized minimal residual (GMRES)<sup>[19]</sup> iteration algorithm is used in this paper to solve these large scale nonlinear structural dynamic equations because of its fast convergence and robust characteristics.

#### 1.3 Structural parallel computation strategy

The nonlinear structural algorithm mainly contains two numerical operating levels<sup>[16]</sup>: Element and system level. The element level uses structural elements and their local nodes to assemble tangent stiffness matrix or force vector, while the system level uses the system nodes to conduct matrix-vector multiplication. Based on these basic numerical operating characteristics, a parallel computation technique is designed here based on the MPI library functions MPI IRecv

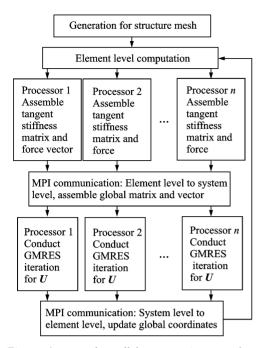


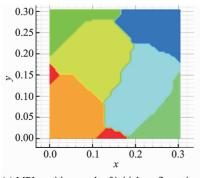
Fig. 1 Structural parallel computation procedure

and MPI\_ISend, as shown in Fig. 1.

#### 1.4 Verification of parallel structural method

The test case is the classical air bag inflation problem. The membrane thickness is  $3.048 \times 10^{-5}$  m and the edge length is 0.3048 m. It is inflated by a constant pressure 23.94 Pa<sup>[18]</sup>. The Young's modulus is 206.8 MPa and the Poisson ratio is 0.30. The time step is  $1.0 \times 10^{-4}$  s and the inflation time is 0.05 s. The partition is made by calling the library functions provided by open source code METIS, which uses node connective relationship to generate balanced logical partition results.

MPI partition result of the initial state is demonstrated in Fig. 2(a). The displacements of numerical simulation (Figs. 2(b,c)) in both the in-plane and transverse directions agree well with those in Ref. [18].



(a) MPI partition result of initial configuration

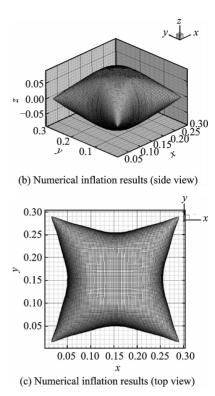


Fig. 2 Air bag inflation case

The structural parallel computation efficiency is demonstrated in Table 1, where the efficiency is defined as the processor number divided by the ratio of the serial run time vs parallel run time<sup>[16]</sup>. The calculation is performed on a HP-Z620 workstation and each processor has a speed of 2, 3 GHz.

Table 1 Grid scale and parallel computation efficiency

	-	-	•
Element	Processor	Computation time/s	Parallel efficiency/%
	Hullibei	tille/ s	efficiency//0
20 000	1	63 510.940	_
20 000	2	35 853.529	88.57
20 000	4	20 649.937	76.89
20 000	8	11 321.835	70.12
12 800	1	60 187.588	
12 800	2	34 738.309	86.63
12 800	4	20 251.545	74.30
12 800	8	11 364.728	66.20

### 2 Time Dependent Aerodynamic Module

#### 2.1 Governing equation for fluid dynamic

The governing equation for the unsteady fluid dynamic model is

$$\iint_{\partial O} [F - G] \, \mathrm{d}S = 0 \tag{6}$$

where  $\Omega$  is the spatial domain for an arbitrary control volume and S its boundary, W the conservative quantities, Q the primitive variables,  $\Gamma$  the Weiss-Smith<sup>[20]</sup> preconditioning matrix which can accelerate the convergence speed for the flow solver at low speeds.  $\Gamma$  and  $\Gamma$  are the convective flux and viscous flux, respectively.

#### 2.2 Time-integration scheme of fluid module

The dual time stepping scheme is employed to provide time-accurate solution of unsteady parachute aerodynamic simulation

$$\left[\frac{\Gamma}{\Delta \tau} + \frac{3}{2\Delta t} \frac{\partial W}{\partial Q}\right] \Delta Q \Omega^{t+\Delta t} = 
- \sum_{m=1}^{N_{\text{face}}} (F_m - G_m) S - 
\frac{(3W_m^{t+\Delta t} \Omega^{t+\Delta t} - 4W_m^t \Omega^t + W_m^{t-\Delta t} \Omega^{t-\Delta t})}{2\Delta t}$$
(7)

where m is stage counter of pseudo time iteration, and  $N_{\text{face}}$  the face number of a control volume. The updating of primitive variables of pseudo time iteration is based on the preconditioned LU-SGS algorithm. The parallel computation strategy of the flow simulation only needs one operating level because only the flow field information of those control volumes near each logical boundaries need to be exchanged among processors. A compatible mesh is generated for the aerodynamic simulation based on the membrane structural mesh on canopy surface.

#### 3 Automatic Mesh Deformation Module

The parachute fluid mesh is treated as a pseudo solid body<sup>[21]</sup> to transform with the large deformation of parachute canopy. The pseudo equilibrium equation governing this dynamic mesh algorithm is

$$\iiint_{\Omega} \mathbf{B}^{\mathrm{T}} \cdot \mathbf{D} \cdot \mathbf{B} \cdot \mathbf{U} d\Omega = 0$$
 (8)

where  $B^T \cdot D \cdot B$  is the pseudo strain tensor, here B and D are the shape function matrix, and material matrix respectively. The shape changes of the canopy are treated as the Dirichlet boundary conditions for the mesh moving solver and the new

grid coordinates can be updated by the pseudo displacement vector U. The parallel computation strategy of this mesh moving algorithm is similar with the structure solver because they both use GMRES algorithm to solve the resulting system equations.

# 4 Parallel Computation Procedure for Parachute FSI Simulation

There are two stages in the FSI simulation: The first stage is the pre-inflation stage which uses a stand-alone nonlinear structure dynamic module to simulate parachute inflation procedure until a fully plump inflated canopy configuration is formed. The second stage is the fluid-structure coupling procedure which couples the nonlinear structure dynamic solver with unsteady preconditioning solver to predict the parachute descent speed as well as parachute configurations. The coupling stage is demonstrated in Fig. 3.

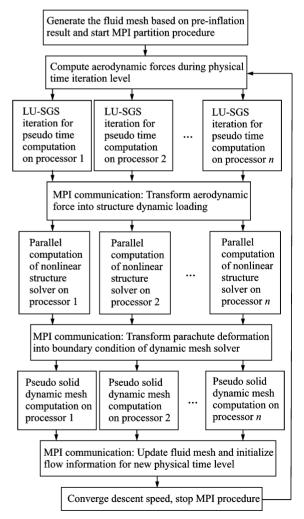


Fig. 3 Parallel computation procedure for ATPS parachute FSI simulation

#### 5 ATPS Parachute FSI Simulation

#### 5.1 ATPS parachute model and pre-inflation

The geometry parameters of the ATPS parachute are set according to Ref. [1] and demonstrated in Table 2. The initial unstressed state is demonstrated in Fig. 4(a). There are 28 suspension lines which are connected to 4 risers and the risers are connected to the payload. The payload is a point mass which has a mass of 100, 697 5 kg<sup>[1]</sup>. The initial descent speed is 4,876 8 m/s<sup>[1]</sup> and the constant inflation-pressure is set to 14,567 2 Pa based on the evaluation of stagnation pressure.

Table 2 ATPS parachute geometrical parameter and material properties

Parameter	Value	Parameter	Value
Top width/m	6.431 28	Arm length/m	3.931 92
Stitching height/m	0.731 52	Bottom edge width/m	6.096 00
Riser lengt/m	1.219 20	Suspension line length/m	6.400 80
Membrane stiffness/Pa	9.564 $8 \times 10^6$	Membrane thickness/m	$3.048 \times 10^{-5}$
Membrane den- sity/(kg • m <sup>-3</sup> ) <sup>1</sup> 223, 509 3		Cable stiffness/Pa	5.342 0×10 <sup>8</sup>
Cable crossse- ctional area/m <sup>2</sup>	$3.11 \times 10^{-6} \mathrm{m}^2$	Cable density/ (kg • m <sup>-3</sup> )	1 223. 509 32

This parachute structure model contains 55 987 nodes and 134 644 elements. Only the bottom node where the four risers join together is constrained as fixed boundary condition. The time step of nonlinear structural simulation is  $5.0\times10^{-4}$  s. After 6 000 nonlinear iterations, the parachute vibration becomes gradually stable, and the ATPS parachute pre-inflation results are demonstrated in Figs. 4 (b—e).

During the inflation stage, the impact energy of pressure loading transforms to unfolding energy and drives the four arms of parachute canopy to separate from the initial unstressed state (0.20 s). After the largest expanding motion (0.40 s), the fabric tension stress starts to spread in the remaining slack zone of parachute canopy (0.80 s), the fight between fabric expending inertia and

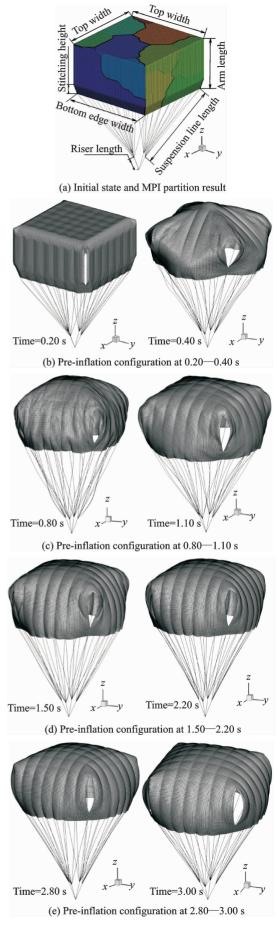


Fig. 4 ATPS parachute pre-inflation simulation

tension stress transforms into the vibration of parachute membrane-cable system (Fig. 4 (c)). As the spreading speed of tension stress gradually catches up with the vibration spreading speed, a dynamic equilibrium state starts to form (Fig. 4 (d)) and the tension stress has changed the canopy shape into a relatively smooth inflated configuration (Fig. 4 (e)).

#### 5.2 FSI simulation of parachute descent stage

A structural fluid mesh containing 3 860 439 hexahedral elements and 3 753 334 grid nodes is generated to conduct the numerical simulation of ATPS parachute aerodynamics (Fig. 5). During the FSI simulation of descent stage, the acceleration and descent speed in the vertical direction can be calculated by the one-degree free fall equations

$$\begin{cases} \ddot{u}_{z}^{t+\Delta t} = \frac{\rho V_{\infty}^{2} A_{r}}{2} \cdot \frac{C_{d}^{t+\Delta t}}{m} - g \\ \dot{u}_{z}^{t+\Delta t} = \dot{u}_{z}^{t} + \ddot{u}_{z}^{t+\Delta t} \cdot \Delta t \end{cases}$$
(9)

where  $V_{\infty}$  and  $A_{\rm r}$  represent initial free stream velocity and reference area, respectively. The reference area of ATPS parachute is set to 41.361 4 m<sup>2</sup> which is equal to the parachute canopy projected area of initial unstressed configuration (Fig. 4 (a)).  $C_{\rm d}$  represents the drag coefficient, m the total mass of parachute-payload system.  $\rho$  and gare the air density and the gravity acceleration, respectively. The physical time step for the aerodynamic simulation is set to 5.  $0 \times 10^{-3}$  s and the structural time step is 5.0 $\times$ 10<sup>-4</sup> s. The FSI simulation of ATPS parachute is carried out on a PC-Cluster with 6 computation nodes and each node has 16 computation threads, the CPU type is Intel® Xeon® E5-2660. The physical time for parachute descent procedure is 5 s and there are 1 000 fluid physical time steps and 10 000 structural nonlinear iterations.

Fig. 6 demonstrates the flow fields of the FSI simulation results. During the FSI simulation of ATPS parachute descent stage, the shape changes of parachute system are smaller than the inflation stage, the breath vibration energy is separated and consumed by the tension stress near the four vents of parachute canopy, and finally reaches a

dynamic equilibrium state. The amount of wrinkles are less than the inflation stage and the shape changes of canopy vents are also smaller than inflation stage, this is because the gradually balanced tension stress formed in inflation stage.

The flow structure can be separated into two main parts: One is the inner stream part which is prevented by parachute canopy and the other is the outer stream part which flow bypass the para-

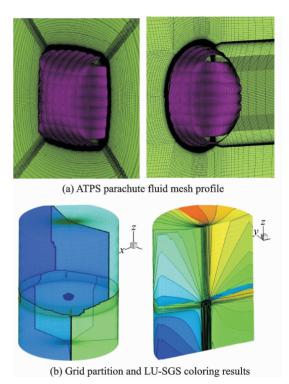


Fig. 5 Fluid mesh of ATPS parachute

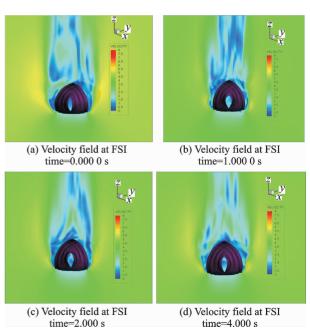


Fig. 6 Flowfields demonstration of FSI simulation

chute canopy. Because the inner stream cannot penetrate the inner surface of parachute canopy, the flow near the center vertical axis has to circle around and form two vortexes, this rotational motion causes an increase of air density and pressure near these areas (Fig. 7 (a)). On one hand, the dissipated kinetic energy during this procedure transforms into expanding energy of parachute canopy. On the other hand, caused by the viscous shearing force and the back flow near the bottom edge of parachute canopy, there forms two separate vortexes due to the rotatory inertia. As time advancing, the vortex position changes from their initial position, but the basic flow structure does not change (Fig. 7(b)). Along with other smaller vortexes formed near parachute canopy, these special vortexes consists the basic structure of parachute flow field and the kinetic energy dissipation caused by this structure transforms into drag force for parachute system.

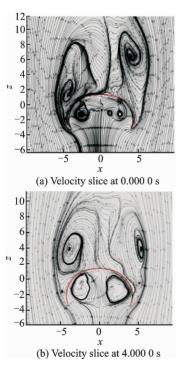


Fig. 7 Slice of parachute flowfield

Fig. 8 demonstrates the FSI simulation results of ATPS parachute descent speed compared with the results provided by Ref. [1]. The near steady descent speed in this paper and Ref. [1] is 4.693 92 m/s and 4.785 36 m/s, respectively. The changes of the descent speed are caused by

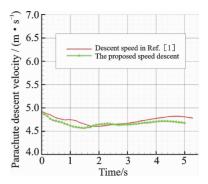


Fig. 8 FSI results of descent speed

the parachute breathe vibration which can be observed during the FSI simulation (Fig. 6).

#### 6 Conclusions

The unsteady preconditioning method coupled with the nonlinear finite element algorithm is applied within MPI parallel computation environment to simulate the ATPS parachute transient dynamics. The FSI simulation of the ATPS parachute is carried out on a PC-Cluster and the result of descent speeds is compared with literature. The simulation result shows that the parachute flow field consists of complex vertex structure and the descent speed is affected by the breathe vibration. Apparently, there are some improvements needed for this parachute FSI simulation method:

- (1) The wrinkles and contact problems during inflation stage need more robust dynamic mesh solver to extend the FSI simulation through entire parachute inflation stage.
- (2) The aerodynamic force of the payload system needs to be computed and the six degree of freedom dynamic equation for the parachute-payload system needs to be studied to simulate the more complex descent problems with asymmetric flow conditions.

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